

Яндекс

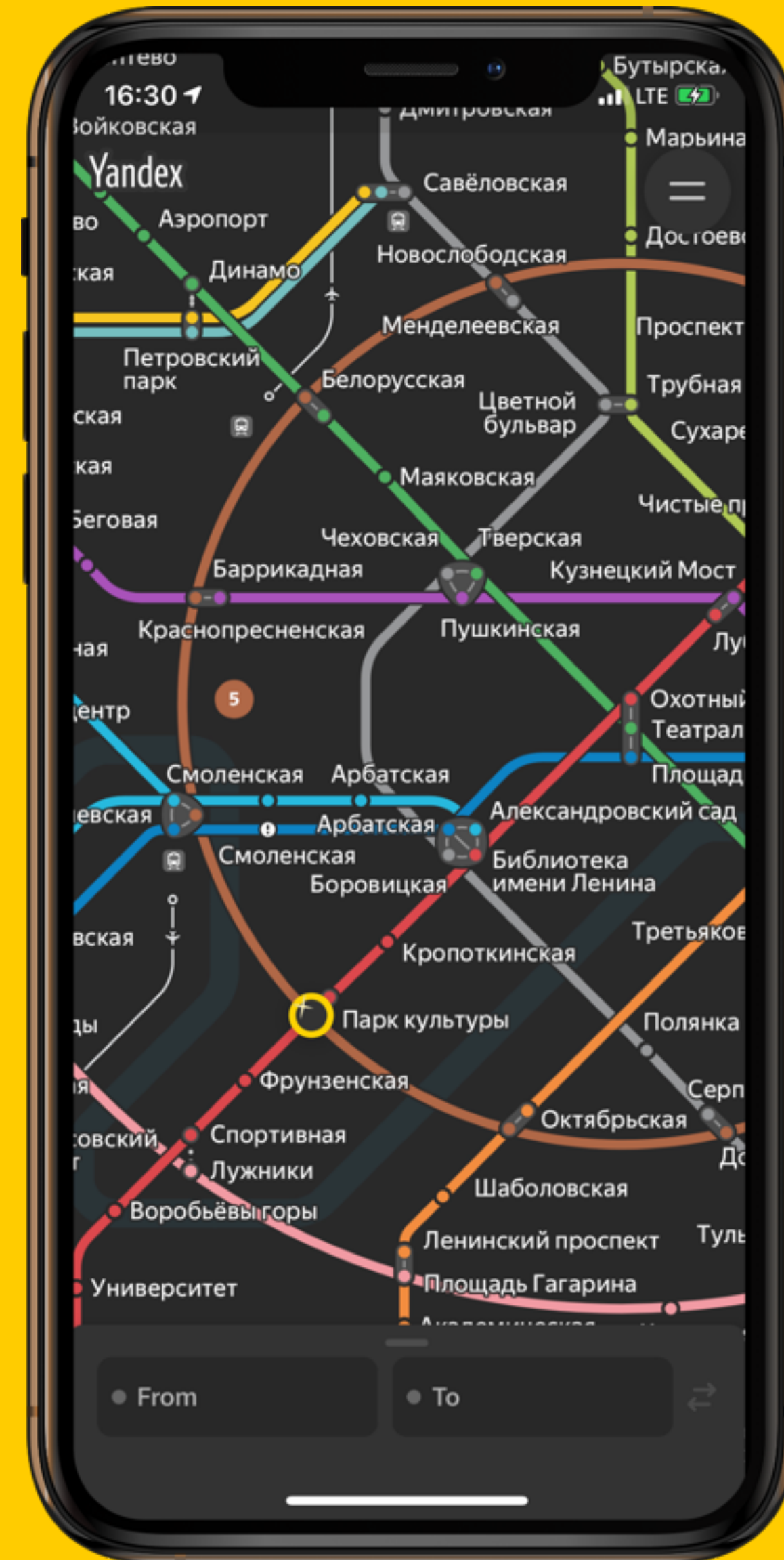
Яндекс

Scroll Mechanics

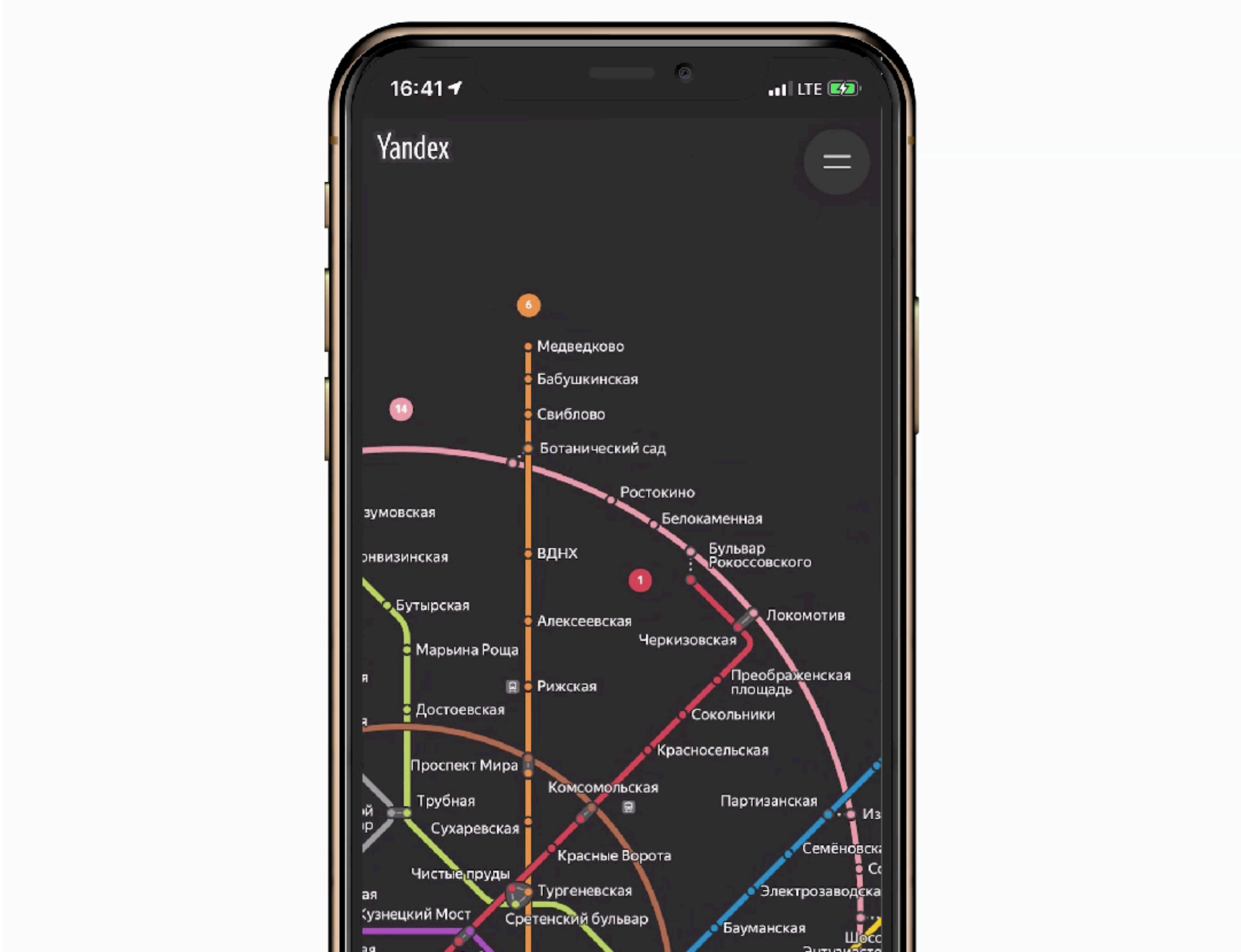
Илья Лобанов

Схема в Яндекс.Метро

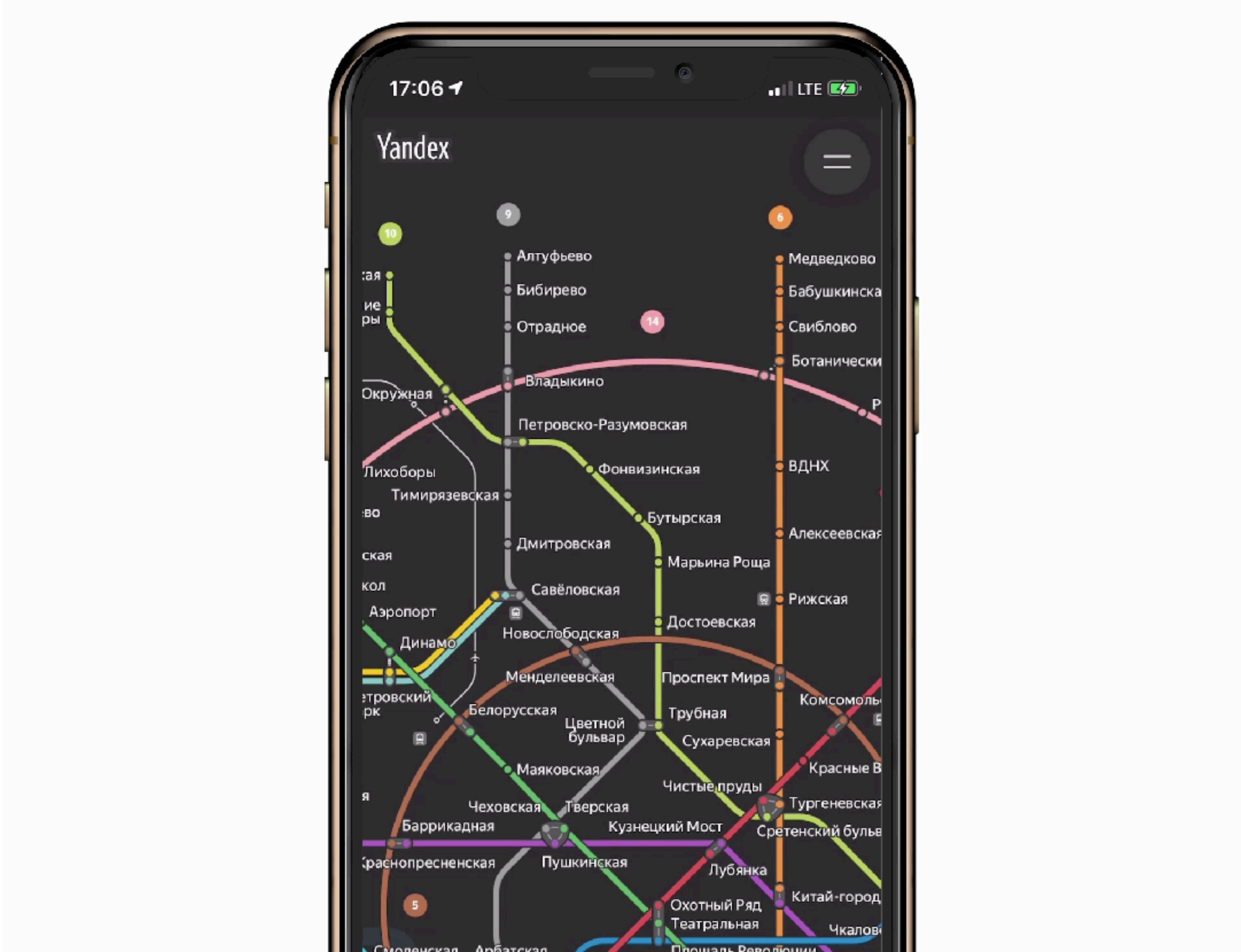
- › Общая библиотека MetroKit для всех платформ
- › Общее поведение скролла схемы
- › В качестве референса был выбран UIScrollView



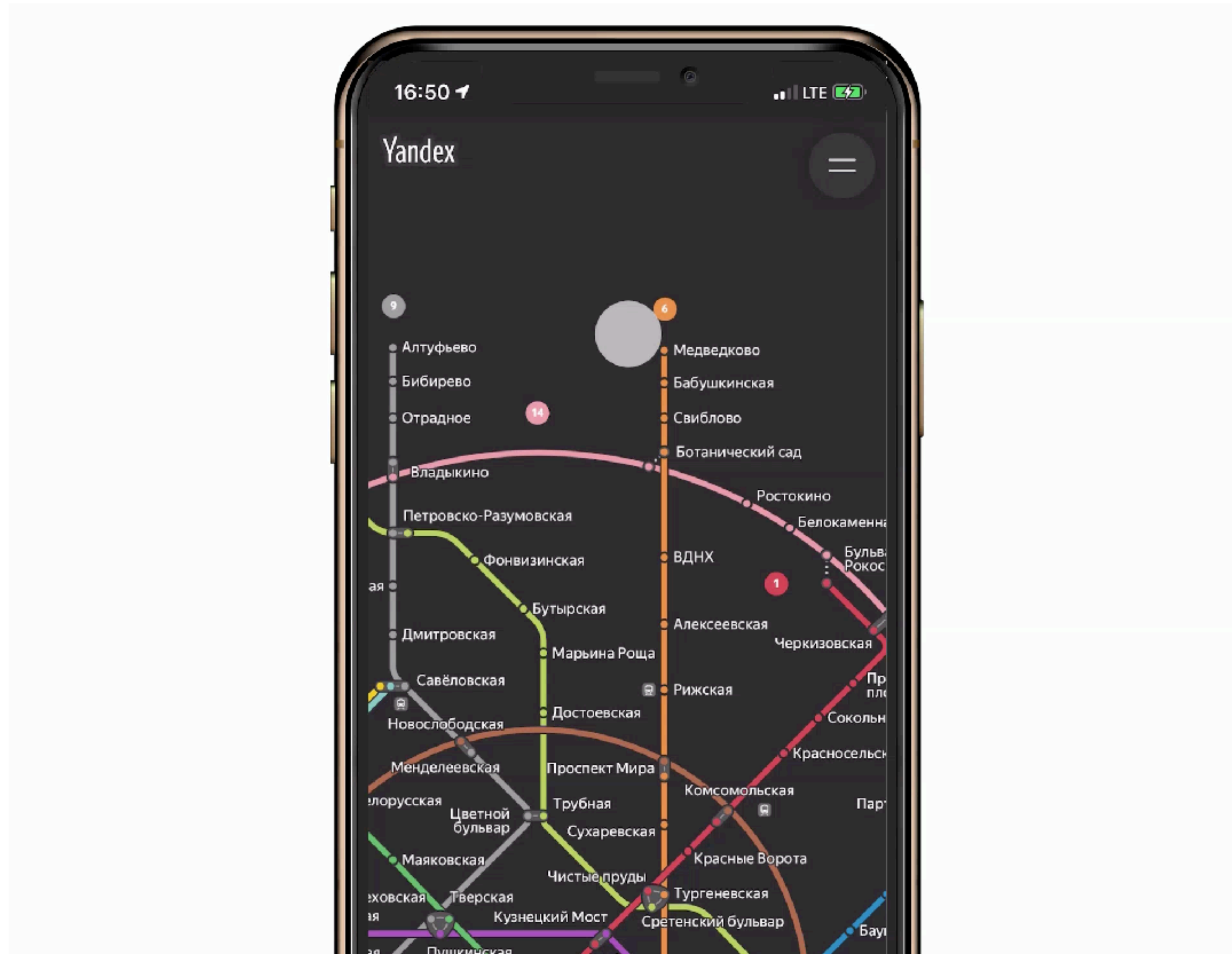
Механики UIScrollView Deceleration



Механики UIScrollView Spring Animation



Механики UIScrollView Rubber Band Effect



Содержание

01 | Тестовый пример

02 | Deceleration

03 | Spring Animation

04 | Rubber Band Effect

05 | Примеры

Тестовый пример

SimpleScrollView

```
class SimpleScrollView: UIView {  
    var contentView: UIView?  
    var contentSize: CGSize  
    var contentOffset: CGPoint  
}
```


SimpleScrollView

```
let panRecognizer = UIPanGestureRecognizer()

override init(frame: CGRect) {
    super.init(frame: frame)
    addGestureRecognizer(panRecognizer)
    panRecognizer.addTarget(self, action: #selector(handlePanRecognizer))
}
```

SimpleScrollView

```
enum State {  
    case `default`  
    case dragging(initialOffset: CGPoint)  
}  
  
var state: State = .default
```

SimpleScrollView

```
@objc func handlePanRecognizer(_ sender: UIPanGestureRecognizer) {  
    switch sender.state {  
    case .began:  
        state = .dragging(initialOffset: contentOffset)  
  
    case .changed:  
        let translation = sender.translation(in: self)  
        if case .dragging(let initialOffset) = state {  
            contentOffset = clampOffset(initialOffset - translation)  
        }  
  
    case .ended:  
        state = .default  
  
    // Other cases  
    }  
}
```

SimpleScrollView

```
var contentOffsetBounds: CGRect {  
    let width = contentSize.width - bounds.width  
    let height = contentSize.height - bounds.height  
    return CGRect(x: 0, y: 0, width: width, height: height)  
}  
  
func clampOffset(_ offset: CGPoint) -> CGPoint {  
    return offset.clamped(to: contentOffsetBounds)  
}
```

SimpleScrollView



Deceleration

Что известно про Deceleration

```
var decelerationRate: UIScrollView.DecelerationRate
```

A floating-point value that determines the rate of deceleration after the user lifts their finger

```
extension UIScrollView.DecelerationRate {  
    static let normal: UIScrollView.DecelerationRate // 0.998  
    static let fast: UIScrollView.DecelerationRate // 0.99  
}
```

Что известно про Deceleration

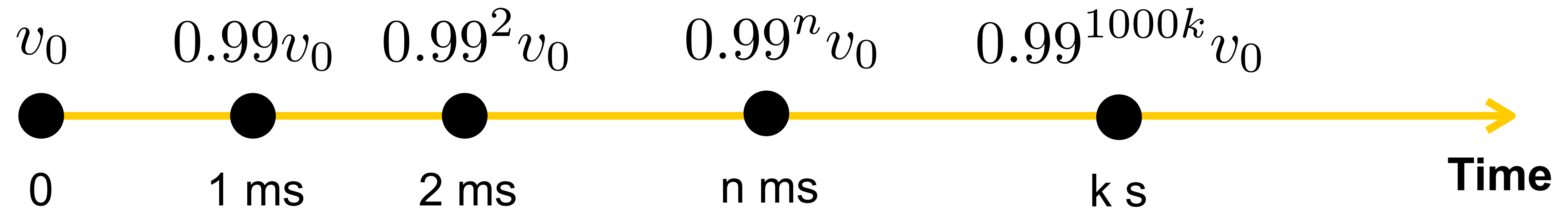
- › Финальная позиция скролла
(Designing Fluid Interfaces — WWDC 2018):

```
// Distance travelled after decelerating to zero velocity at a constant rate.  
func project(initialVelocity: Float, decelerationRate: Float) -> Float {  
    return (initialVelocity / 1000.0) * decelerationRate / (1.0 - decelerationRate)  
}
```

Изменение скорости

Deceleration Rate

.fast = 0.99



Функция скорости

$$v(t) = v_0 d^{1000t}$$

- › v — скорость, pt/s
- › v_0 — начальная скорость, pt/s
- › d — коэффициент замедления ($0 < d < 1$)
- › t — время, s

Уравнение движения

$$x(t) = ?$$

$$x(t) = x_0 + \int_0^t v(x) dx$$

x_0 — начальное положение точки

Уравнение движения

$$x(t) = x_0 + v_0 \int_0^t d^{1000x} dx$$

$$x(t) = x_0 + v_0 \frac{d^{1000t} - 1}{1000 \ln(d)}$$

Конечная точка

$$X = \lim_{t \rightarrow \infty} x(t) = \lim_{t \rightarrow \infty} \left(x_0 + v_0 \frac{d^{1000t} - 1}{1000 \ln(d)} \right)$$

$$X = x_0 - \frac{v_0}{1000 \ln(d)}$$

Конечная точка

$$X = x_0 - \frac{v_0}{1000 \ln(d)}$$

Apple:

$$X = x_0 + \frac{v_0 d}{1000(1 - d)}$$

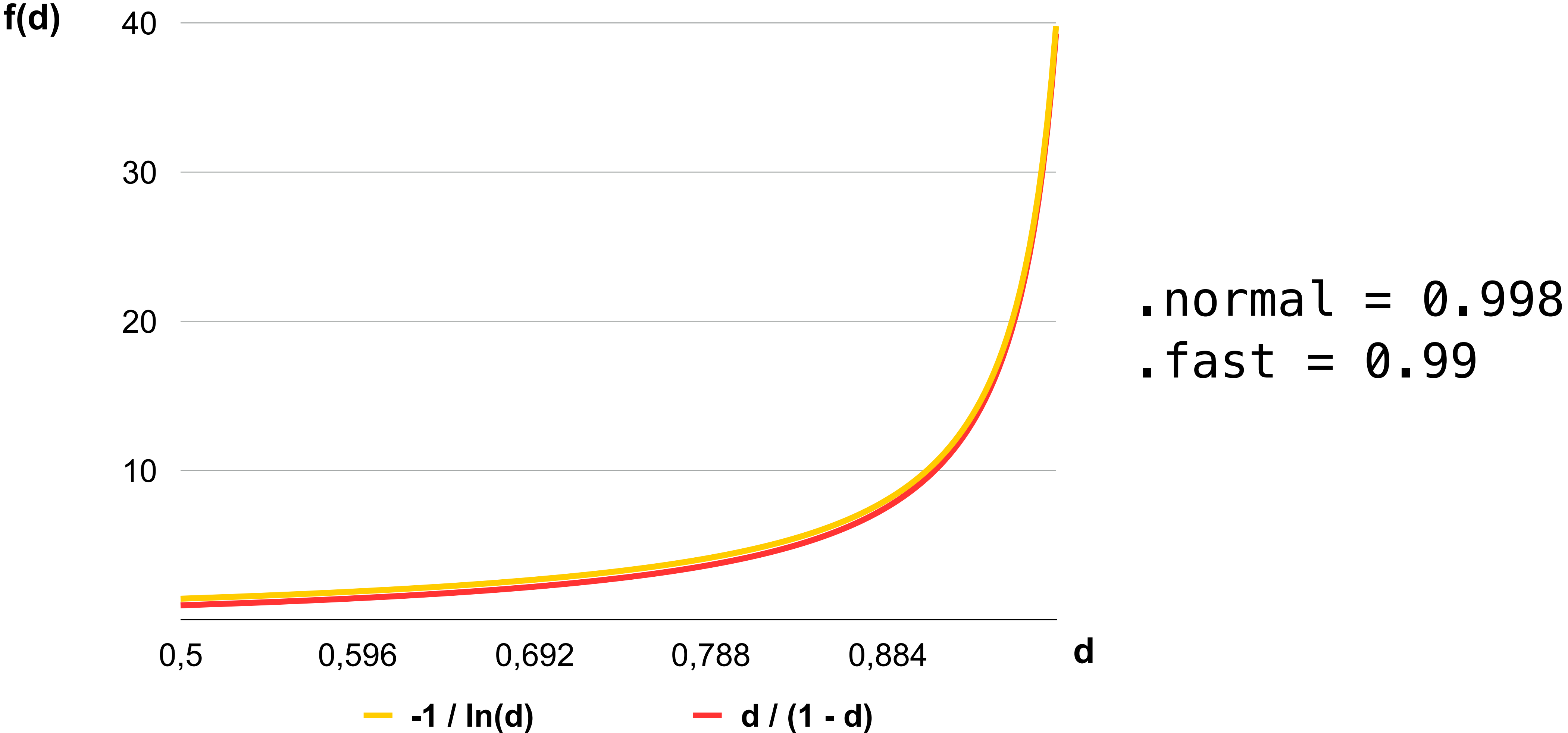
Сравнение с формулой от Apple

$$\frac{-1}{\ln(d)} \quad \text{vs} \quad \frac{d}{1-d}$$

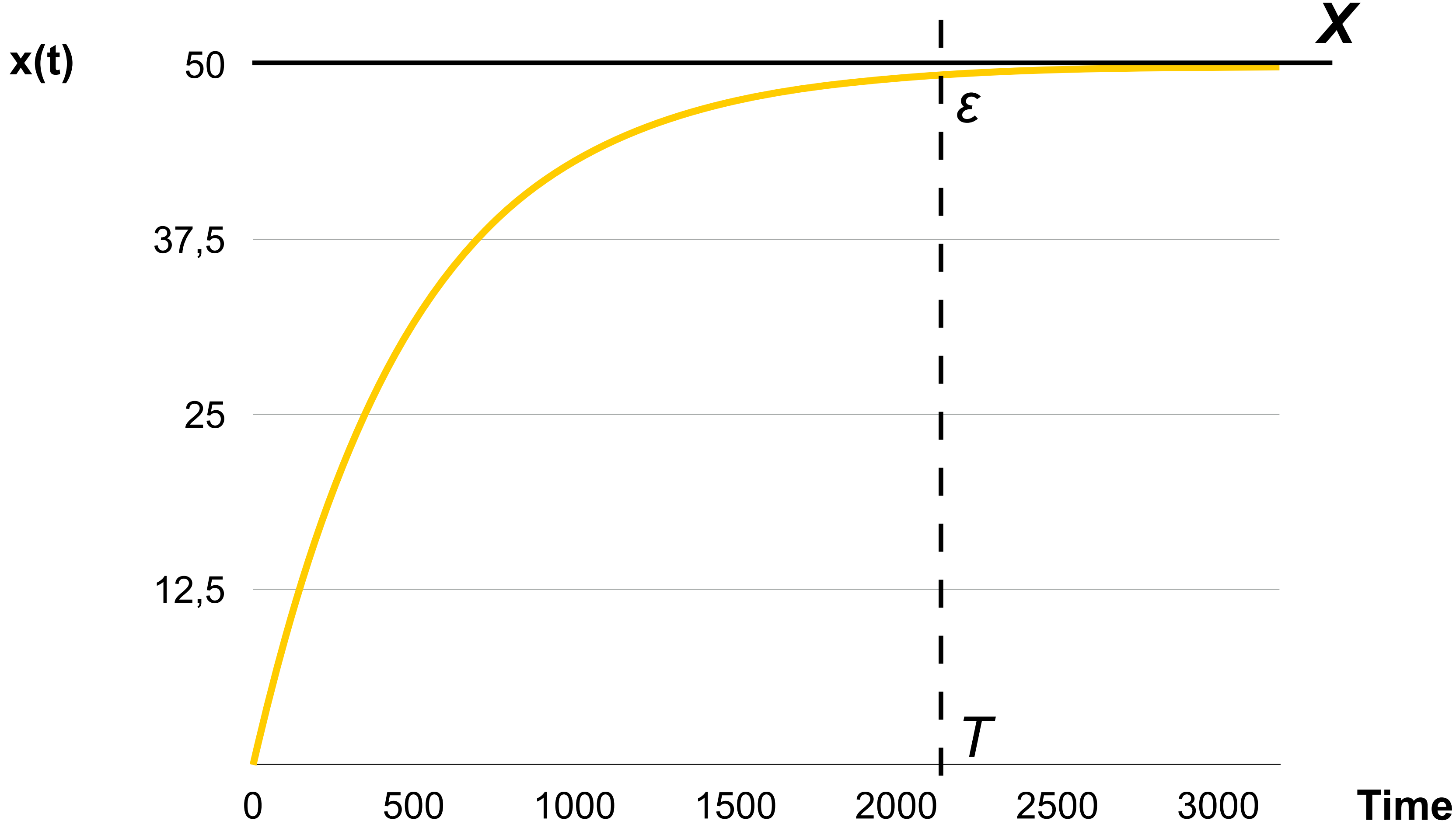
› Разложение натурального логарифма в ряд Тейлора:

$$\ln(x) = \frac{x-1}{x} + \frac{(x-1)^2}{2x^2} + \dots$$

Сравнение с формулой от Apple



Время движения



Время движения

$$|X - x(T)| = \varepsilon$$

$$T = \frac{\ln\left(\frac{-1000\varepsilon \ln(d)}{|v_0|}\right)}{1000 \ln(d)}$$

DecelerationTimingParameters

```
struct DecelerationTimingParameters {  
    var initialValue: CGPoint  
    var initialVelocity: CGPoint  
    var decelerationRate: CGFloat  
    var threshold: CGFloat  
}  
  
extension DecelerationTimingParameters {  
    var destination: CGPoint  
    var duration: TimeInterval  
    func value(at time: TimeInterval) -> CGPoint  
}
```

TimerAnimation

```
class TimerAnimation {  
    typealias Animations = (_ progress: Double, _ time: TimeInterval) -> Void  
    typealias Completion = (_ finished: Bool) -> Void  
  
    init(duration: TimeInterval, animations: @escaping Animations,  
         completion: Completion? = nil)  
}
```

SimpleScrollView

```
@objc func handlePanRecognizer(_ sender: UIPanGestureRecognizer) {
    switch sender.state {
    case .began:
        state = .dragging(initialOffset: contentOffset)

    case .changed:
        let translation = sender.translation(in: self)
        if case .dragging(let initialOffset) = state {
            contentOffset = clampOffset(initialOffset - translation)
        }

    case .ended:
        state = .default

    // Other cases
    }
}
```

SimpleScrollView

```
@objc func handlePanRecognizer(_ sender: UIPanGestureRecognizer) {  
    switch sender.state {  
    case .began:  
        state = .dragging(initialOffset: contentOffset)  
  
    case .changed:  
        let translation = sender.translation(in: self)  
        if case .dragging(let initialOffset) = state {  
            contentOffset = clampOffset(initialOffset - translation)  
        }  
  
    case .ended:  
        state = .default  
        let velocity = sender.velocity(in: self)  
        startDeceleration(withVelocity: -velocity)  
  
    // Other cases  
    }  
}
```


SimpleScrollView

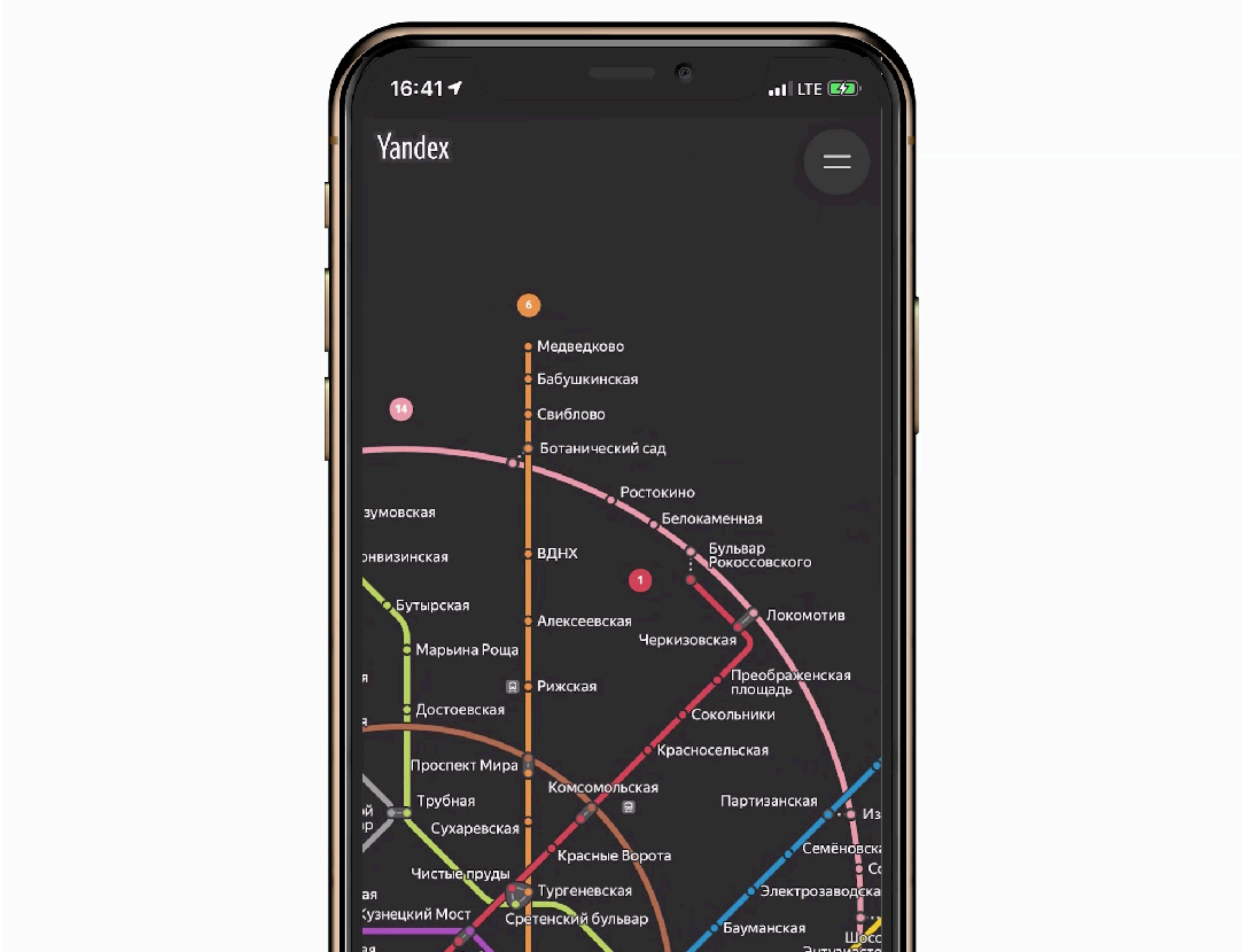
```
var contentOffsetAnimation: TimerAnimation?

func startDeceleration(withVelocity velocity: CGPoint) {
    let decelerationRate = UIScrollView.DecelerationRate.normal.rawValue
    let threshold = 0.5 / UIScreen.main.scale

    let parameters = DecelerationTimingParameters(initialValue: contentOffset,
                                                    initialVelocity: velocity,
                                                    decelerationRate: decelerationRate,
                                                    threshold: threshold)

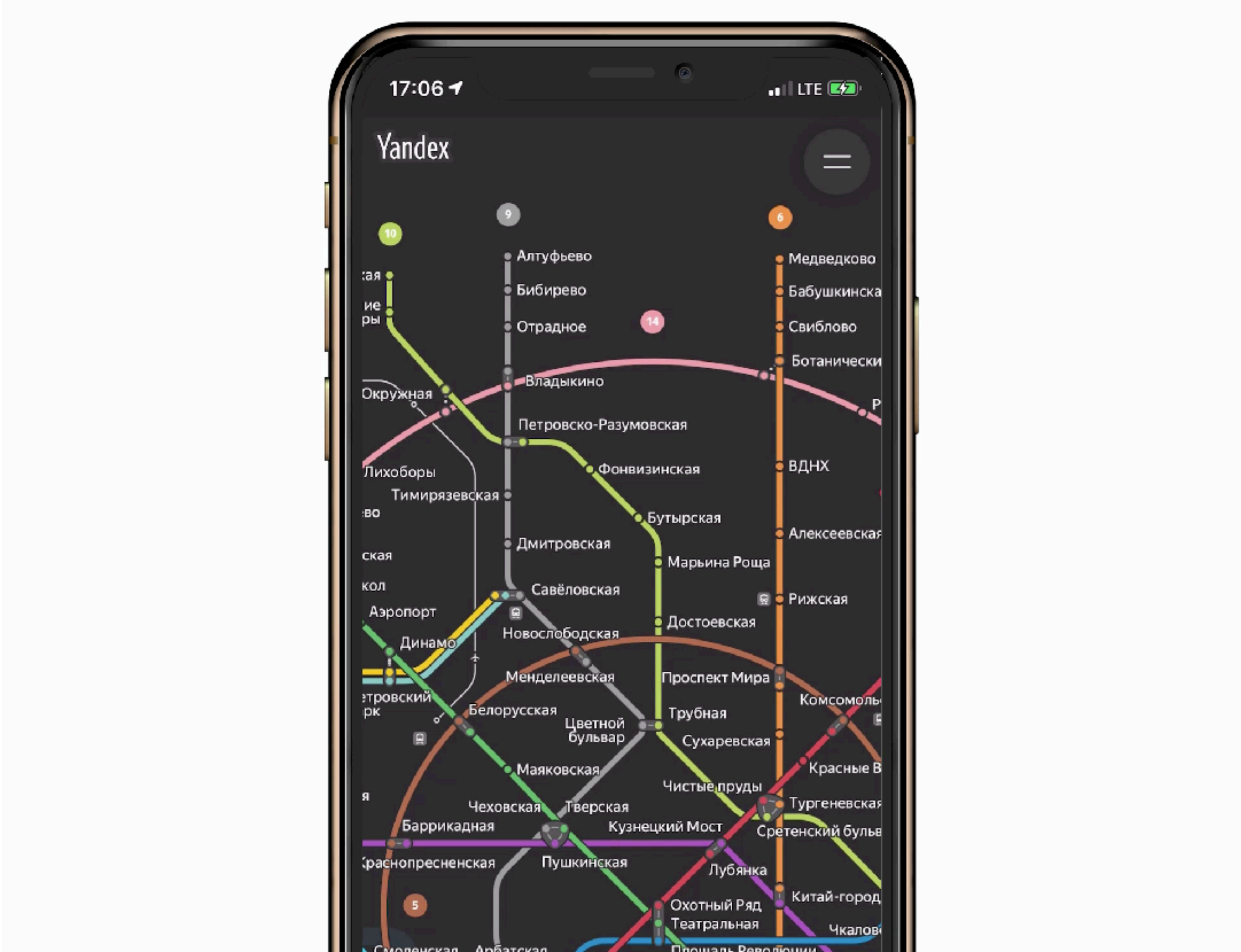
    contentOffsetAnimation = TimerAnimation(
        duration: parameters.duration,
        animations: { [weak self] _, time in
            guard let self = self else { return }
            self.contentOffset = self.clampOffset(parameters.value(at: time))
        })
}
```

Deceleration



Spring Animation

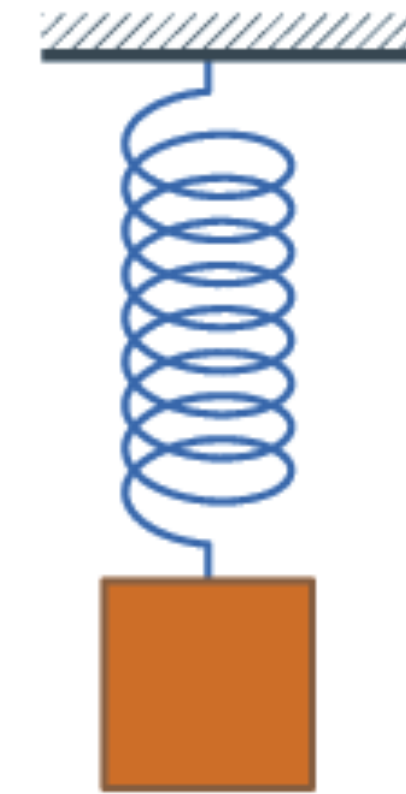
Spring Animation



Spring Animation

- › m — масса (mass)
- › k — жесткость (stiffness)
- › d — затухание (damping)
или
- › ζ — коэффициент затухания (damping ratio)

$$\zeta = \frac{d}{2\sqrt{km}}$$



Уравнение движения

$$m \frac{d^2 x}{dt^2} + d \frac{dx}{dt} + kx = 0$$

- › m — масса (mass)
- › k — жесткость (stiffness)
- › d — затухание (damping)

Damping Ratio ζ

0.1



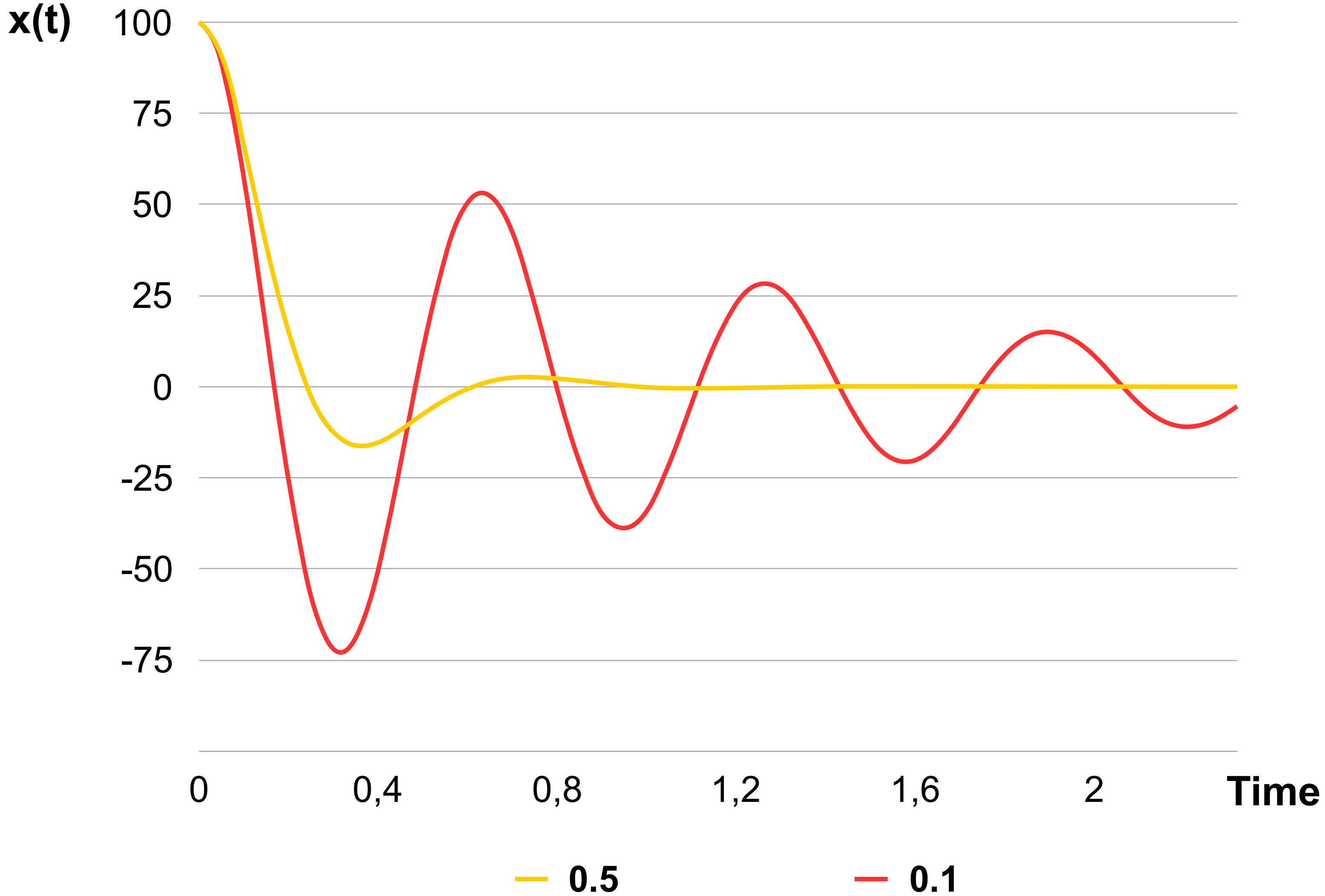
0.5



1.0

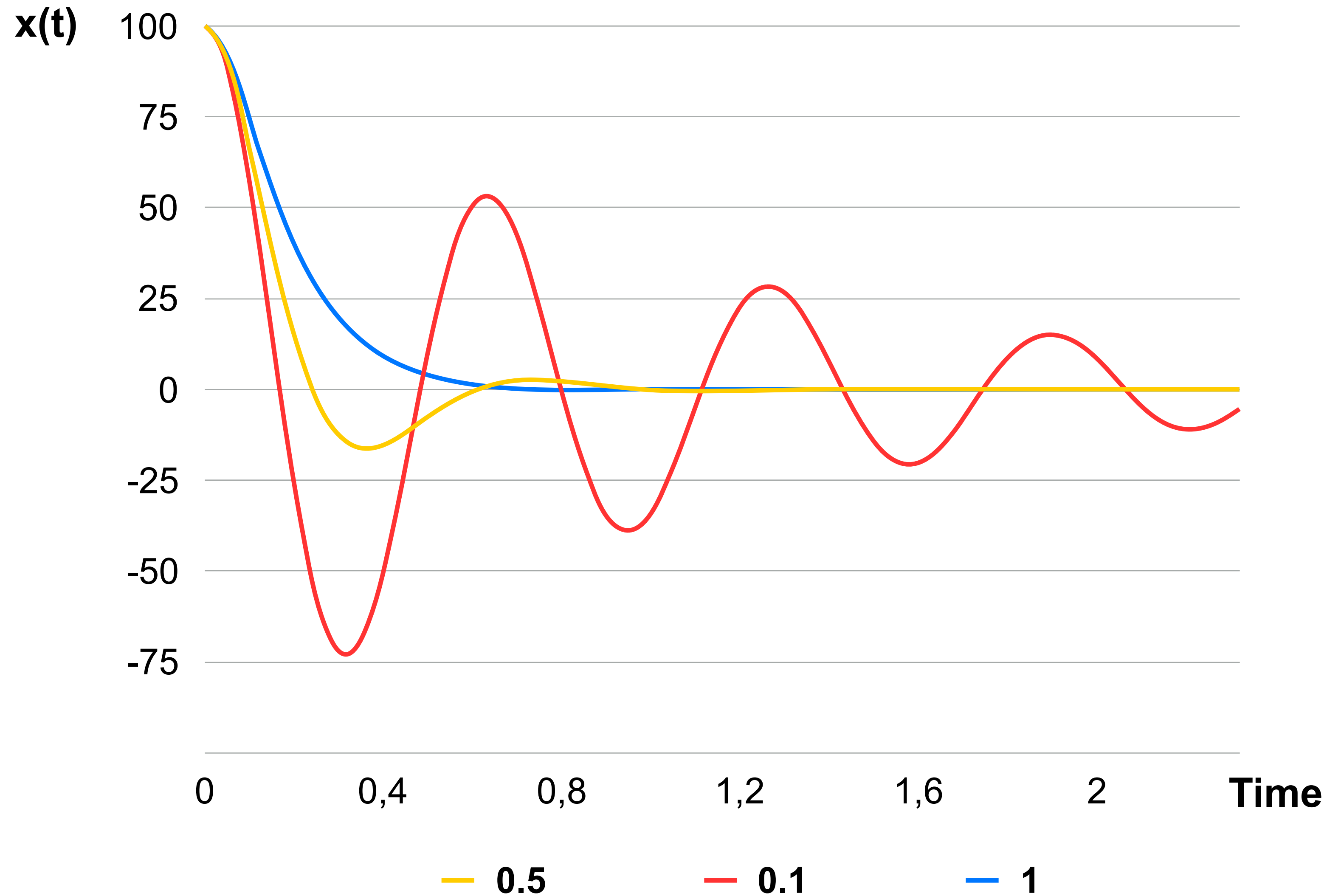


Damping Ratio ζ



› Слабое затухание
(Underdamped)
 $0 < \zeta < 1$

Damping Ratio ζ



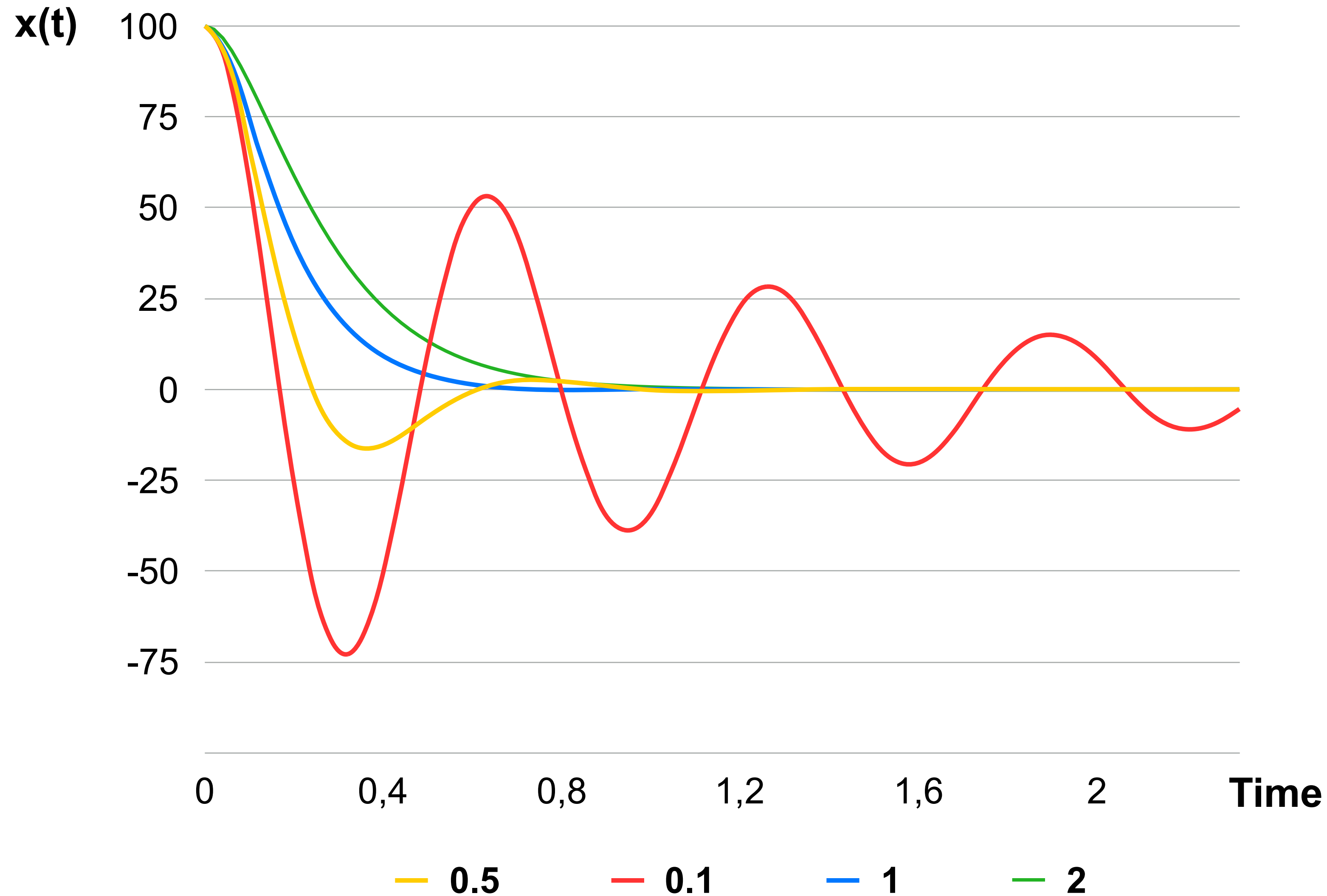
› Слабое затухание
(Underdamped)

$$0 < \zeta < 1$$

› Граница апериодичности
(Critically damped)

$$\zeta = 1$$

Damping Ratio ζ



› Слабое затухание
(Underdamped)

$$0 < \zeta < 1$$

› Граница апериодичности
(Critically damped)

$$\zeta = 1$$

› Апериодичность
(Overdamped)

$$\zeta > 1$$

Уравнение движения

$$m \frac{d^2 x}{dt^2} + d \frac{dx}{dt} + kx = 0$$

› Уравнение движения

$$x(t) = ?$$

› Время колебаний

$$T = ?$$

Уравнение движения

Слабое затухание ($0 < \zeta < 1$)

$$x(t) = (C_1 \cos \omega' t + C_2 \sin \omega' t) e^{-\beta t}$$

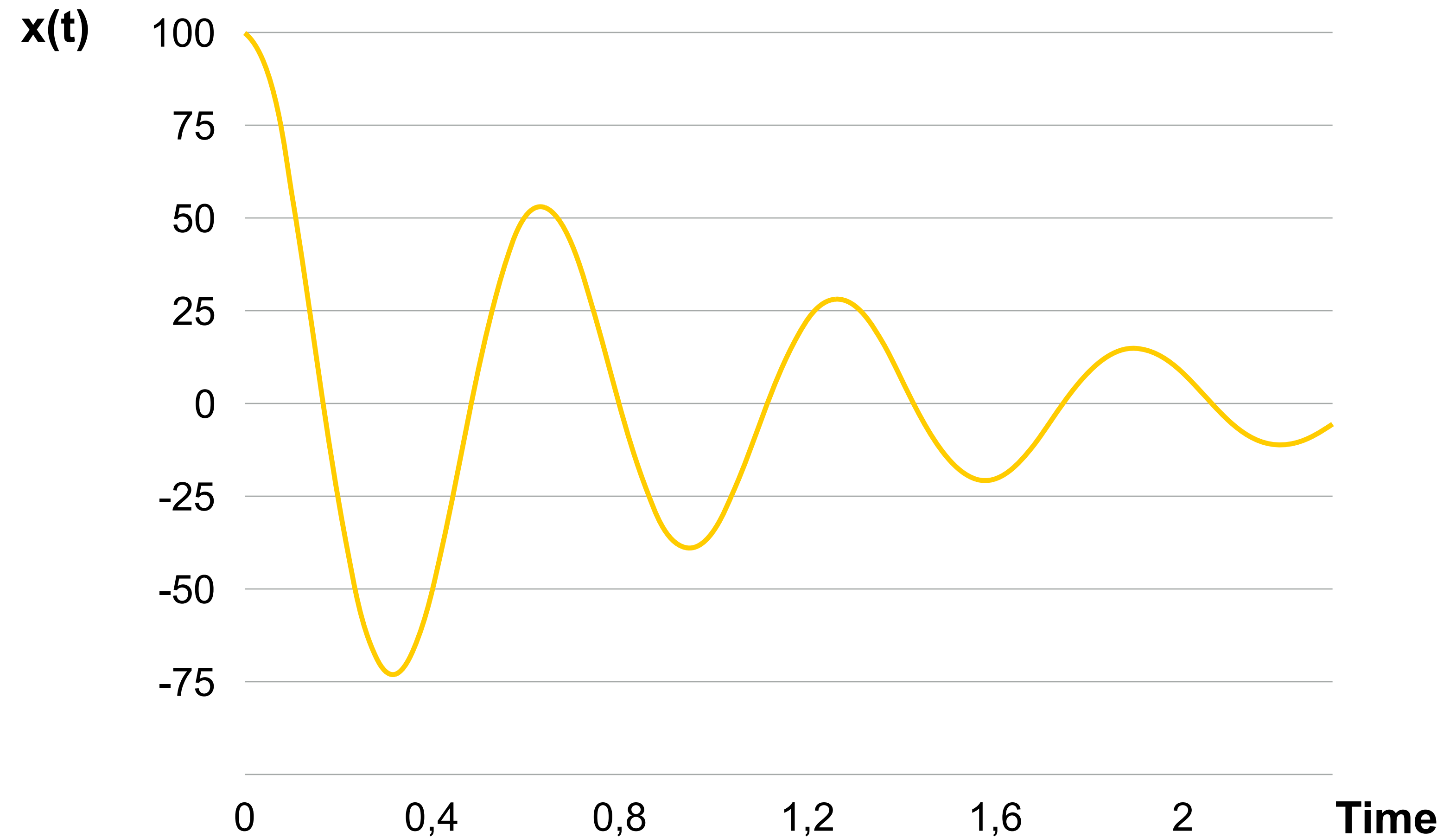
ω' — собственная частота системы
(damped natural frequency)

$$\beta = \frac{d}{2m}$$

$$\begin{aligned} x(0) = x_0 \\ x'(0) = v_0 \end{aligned} \Rightarrow \begin{aligned} C_1 &= x_0 \\ C_2 &= \frac{v_0 + \beta x_0}{\omega'} \end{aligned}$$

Уравнение движения

Слабое затухание ($0 < \zeta < 1$)



Уравнение движения

Граница апериодичности ($\zeta = 1$)

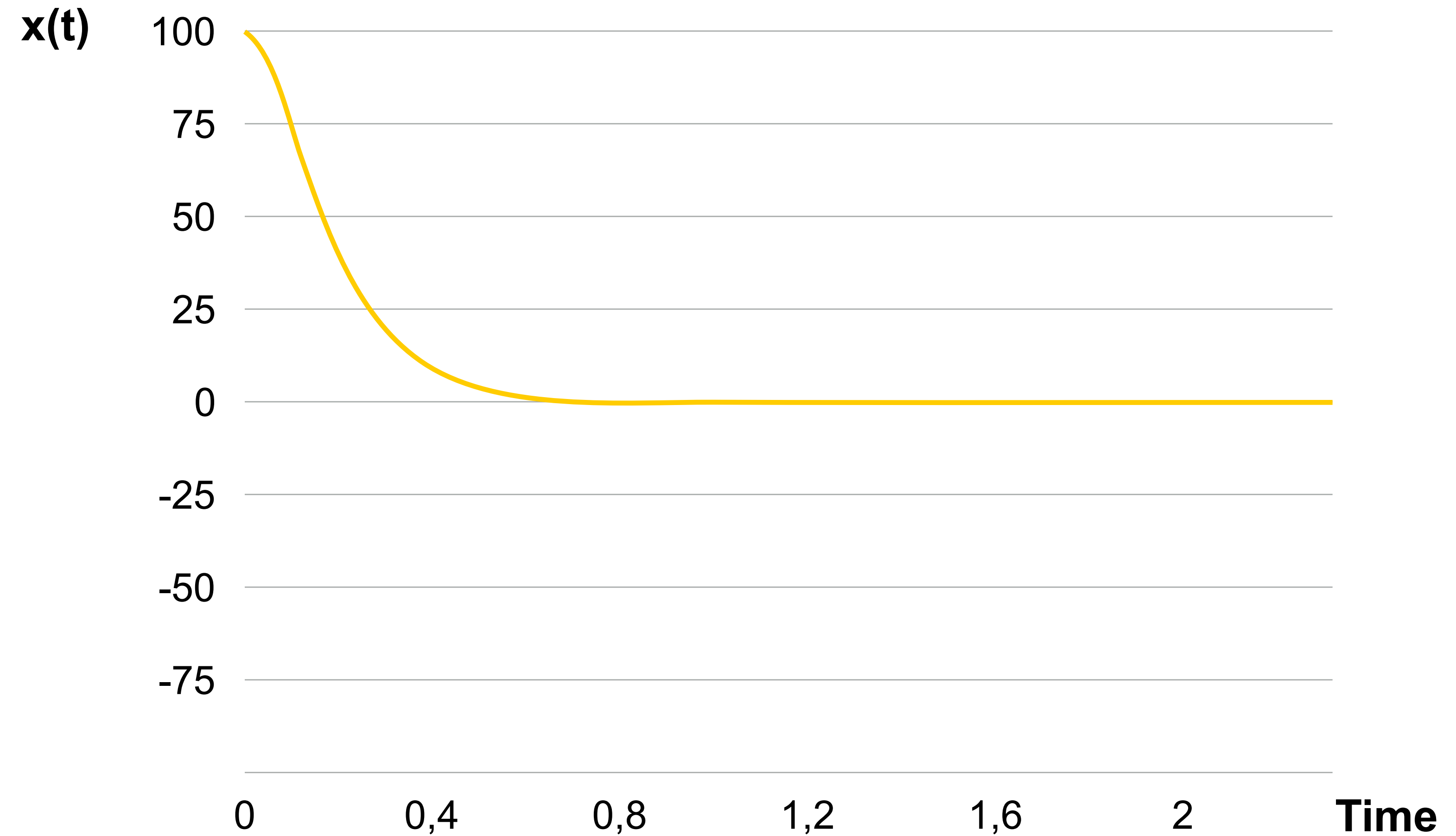
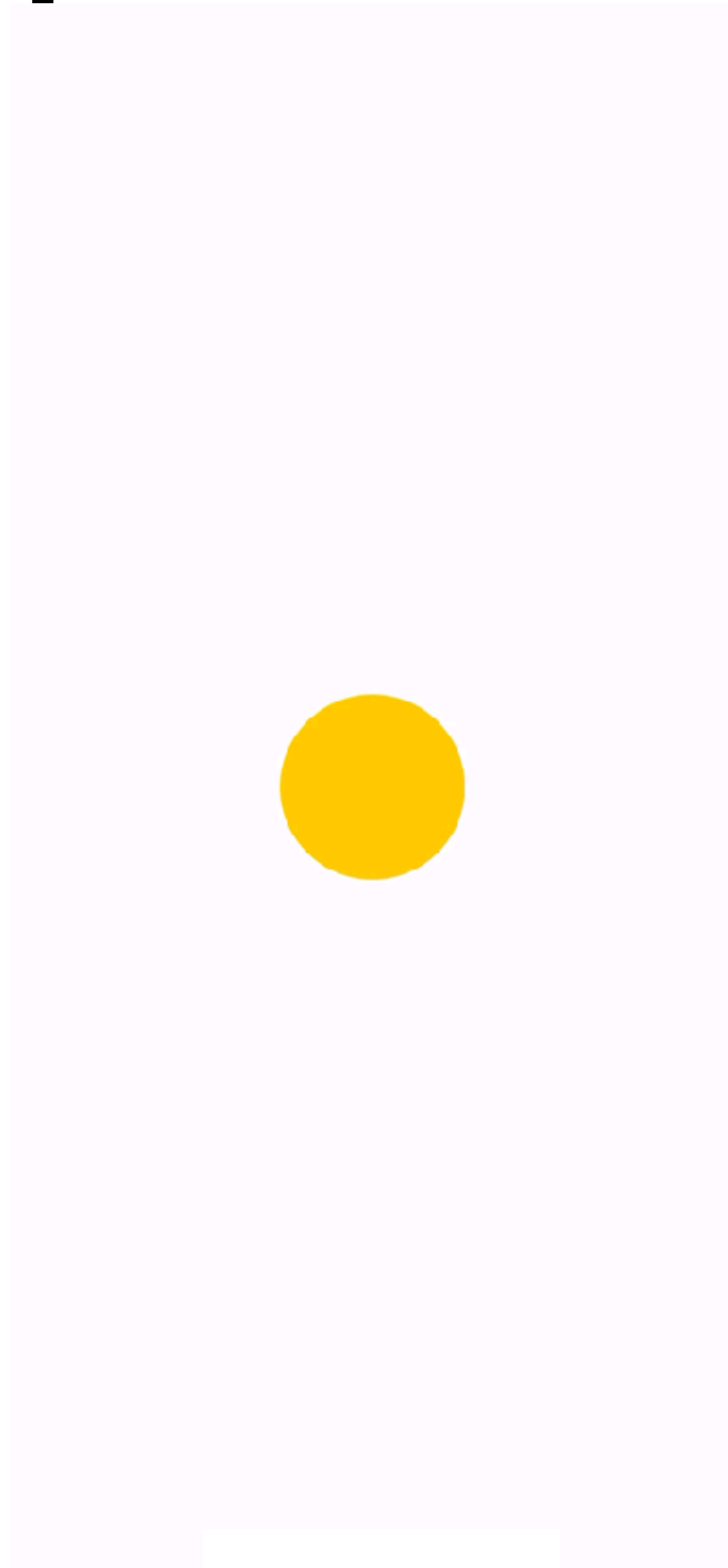
$$x(t) = (C_1 + C_2 t)e^{-\beta t}$$

$$\beta = \frac{d}{2m}$$

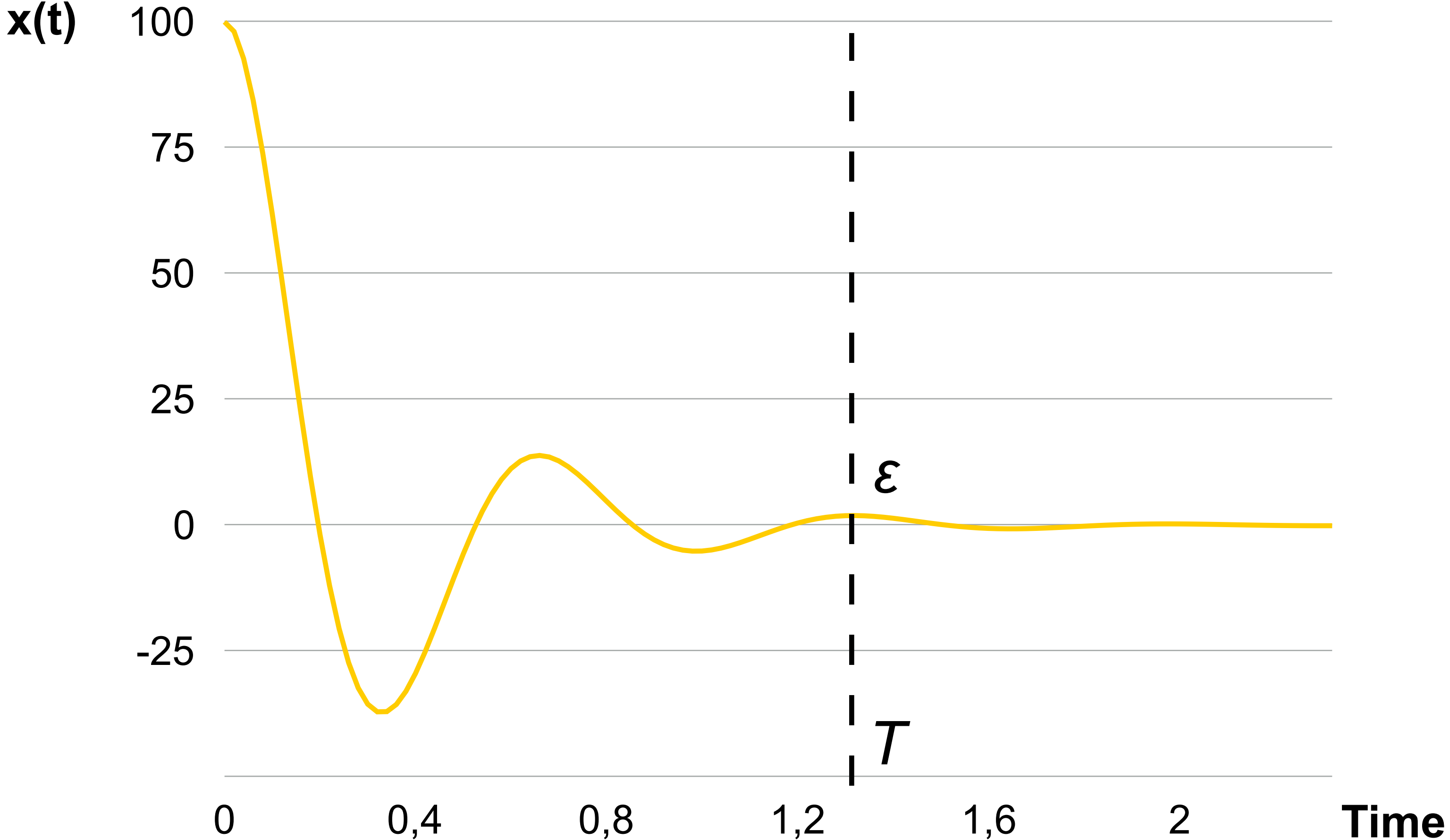
$$\begin{aligned} x(0) = x_0 & \Rightarrow C_1 = x_0 \\ x'(0) = v_0 & \Rightarrow C_2 = v_0 + \beta x_0 \end{aligned}$$

Уравнение движения

Граница апериодичности ($\zeta = 1$)



Время колебаний



Время колебаний

Слабое затухание ($0 < \zeta < 1$)

$$T = \frac{1}{\beta} \ln \frac{|C_1| + |C_2|}{\varepsilon}$$

$$\beta = \frac{d}{2m}$$

$$C_1 = x_0$$

$$C_2 = \frac{v_0 + \beta x_0}{\omega'}$$

Время колебаний

Граница апериодичности ($\zeta = 1$)

$$T = \max\left(\frac{1}{\beta} \ln \frac{2|C_1|}{\varepsilon}, \frac{2}{\beta} \ln \frac{4|C_2|}{e\beta\varepsilon}\right)$$

$$\beta = \frac{d}{2m}$$

$$C_1 = x_0$$

$$C_2 = v_0 + \beta x_0$$

Spring Animations B iOS SDK UIView

```
extension UIView {  
    class func animate(withDuration: TimeInterval,  
                        delay: TimeInterval,  
                        usingSpringWithDamping dampingRatio: CGFloat,  
                        initialSpringVelocity velocity: CGFloat,  
                        options: UIView.AnimationOptions = [],  
                        animations: @escaping () -> Void,  
                        completion: ((Bool) -> Void)? = nil)  
}
```

Spring Animations B iOS SDK

CASpringAnimation

```
open class CASpringAnimation : CABasicAnimation {  
  
    /* The mass of the object attached to the end of the spring. Must be greater  
       than 0. Defaults to one. */  
    open var mass: CGFloat  
  
    /* The spring stiffness coefficient. Must be greater than 0.  
       * Defaults to 100. */  
    open var stiffness: CGFloat  
  
    /* The damping coefficient. Must be greater than or equal to 0.  
       * Defaults to 10. */  
    open var damping: CGFloat  
  
}
```

Spring Animations B iOS SDK

CASpringAnimation

```
extension CASpringAnimation {  
  
    convenience init(mass: CGFloat = 1, stiffness: CGFloat = 100,  
                    dampingRatio: CGFloat)  
    {  
        self.init()  
  
        self.mass = mass  
        self.stiffness = stiffness  
        self.damping = 2 * dampingRatio * sqrt(mass * stiffness)  
    }  
  
}
```

Spring Animations в iOS SDK

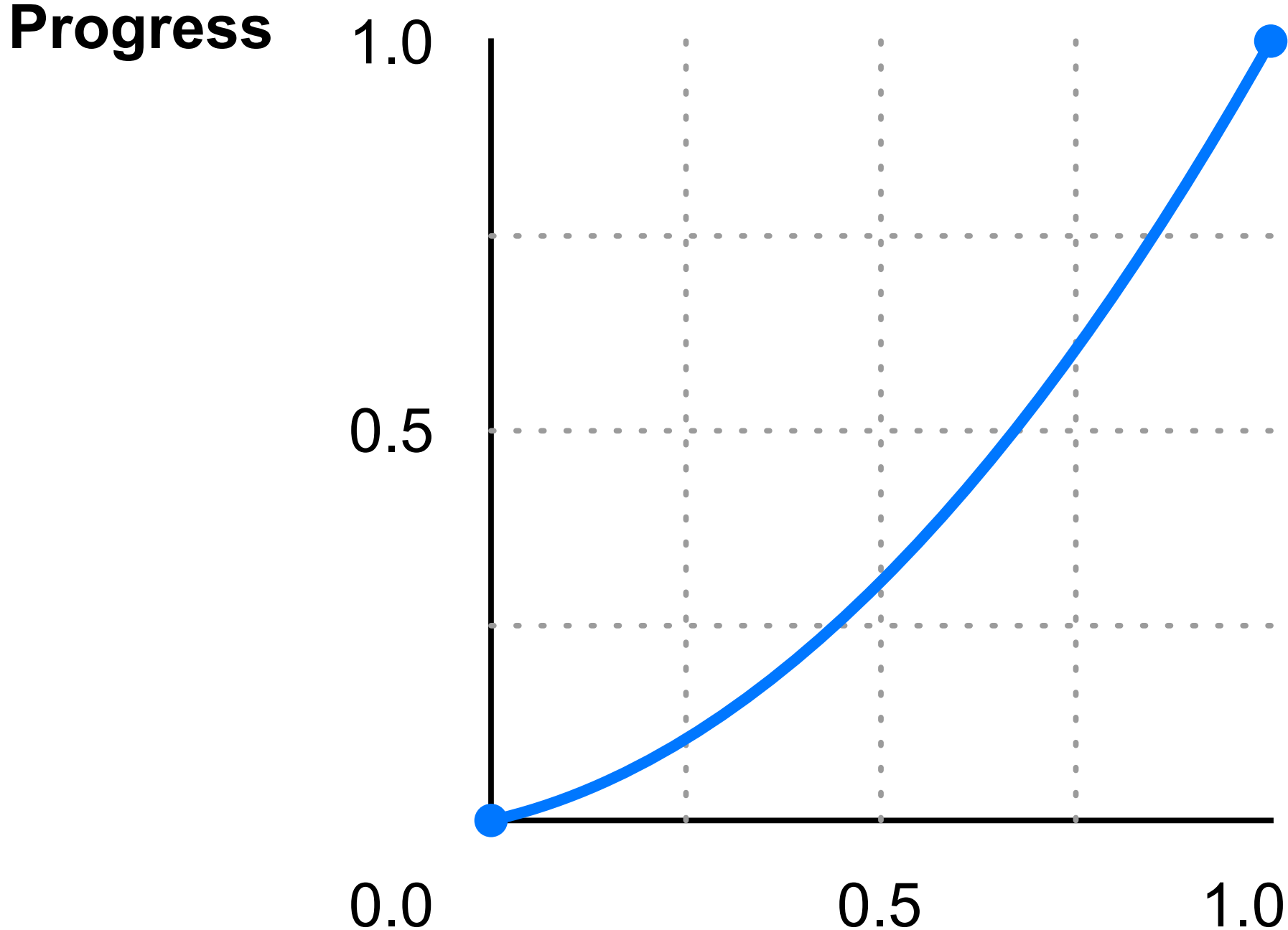
CASpringAnimation

```
open class CASpringAnimation : CABasicAnimation {  
  
    /* The basic duration of the object. Defaults to 0. */  
    var duration: CFTimeInterval { get set }  
  
    /* Returns the estimated duration required for the spring system to be  
     * considered at rest. The duration is evaluated for the current animation  
     * parameters. */  
    open var settlingDuration: CFTimeInterval { get }  
  
}
```

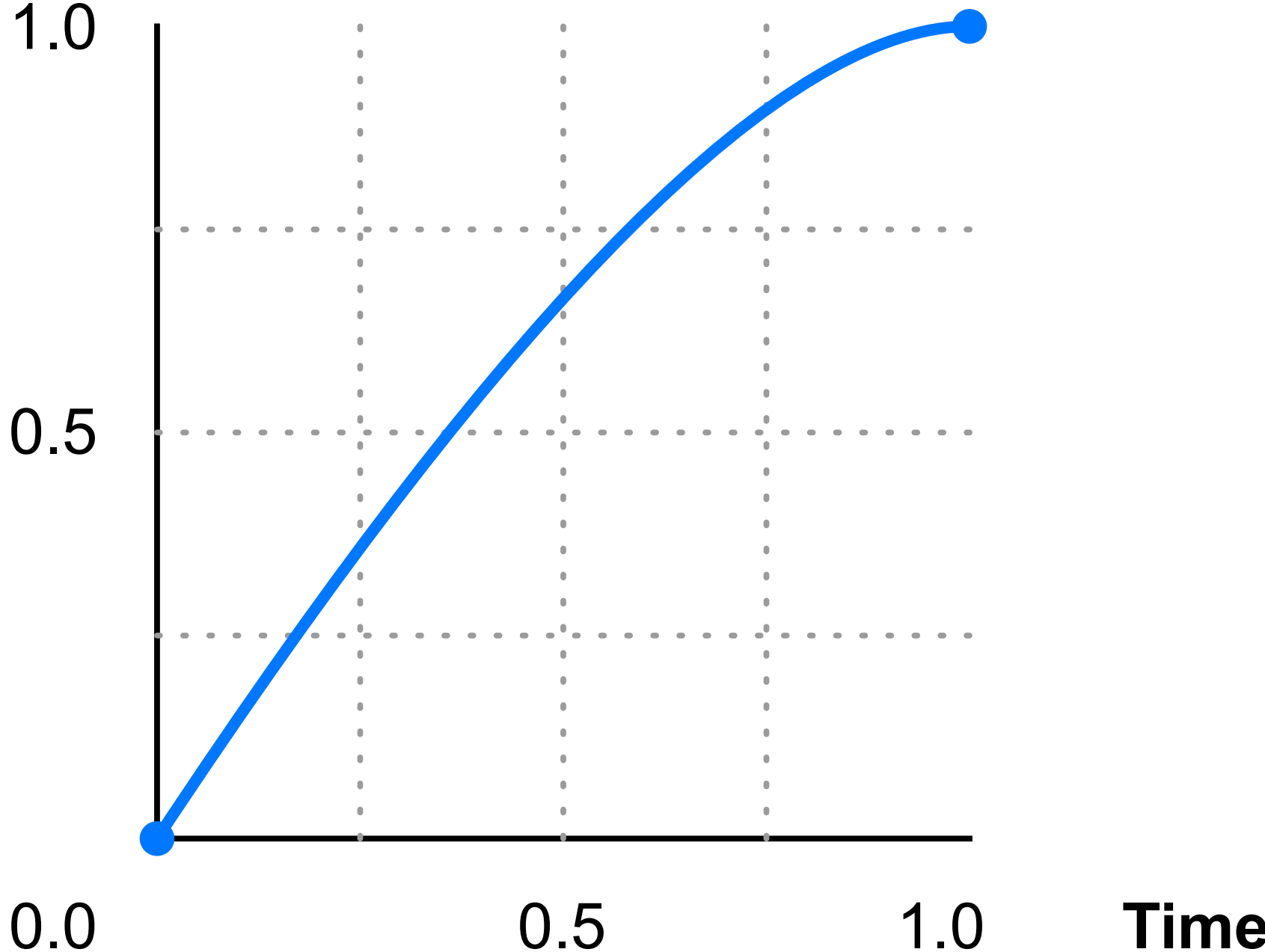
› **settlingDuration** не учитывает смещение пружины:
fromValue и **toValue**

Spring Animations B iOS SDK

Ease In



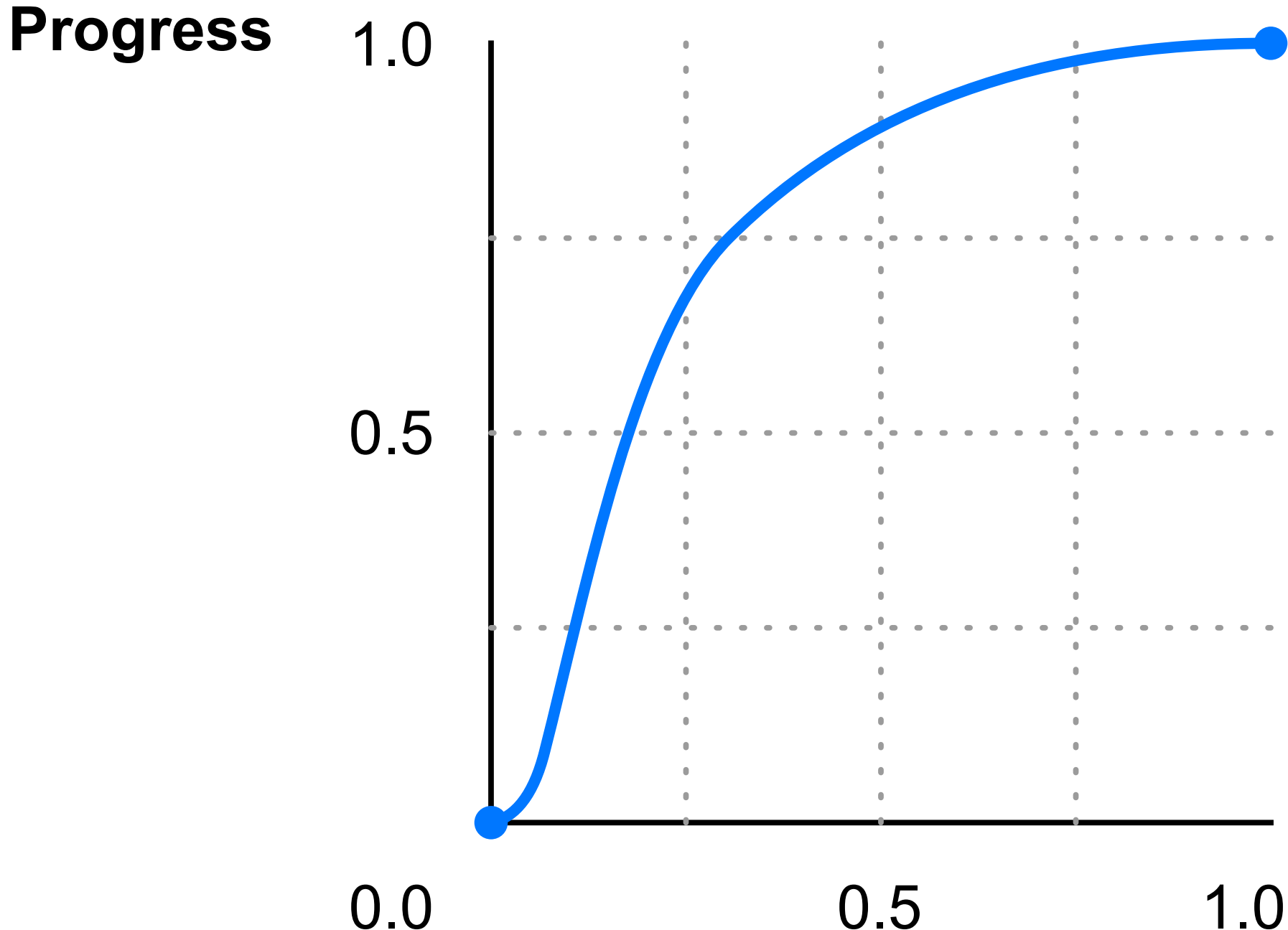
Ease Out



Spring Animations in iOS SDK

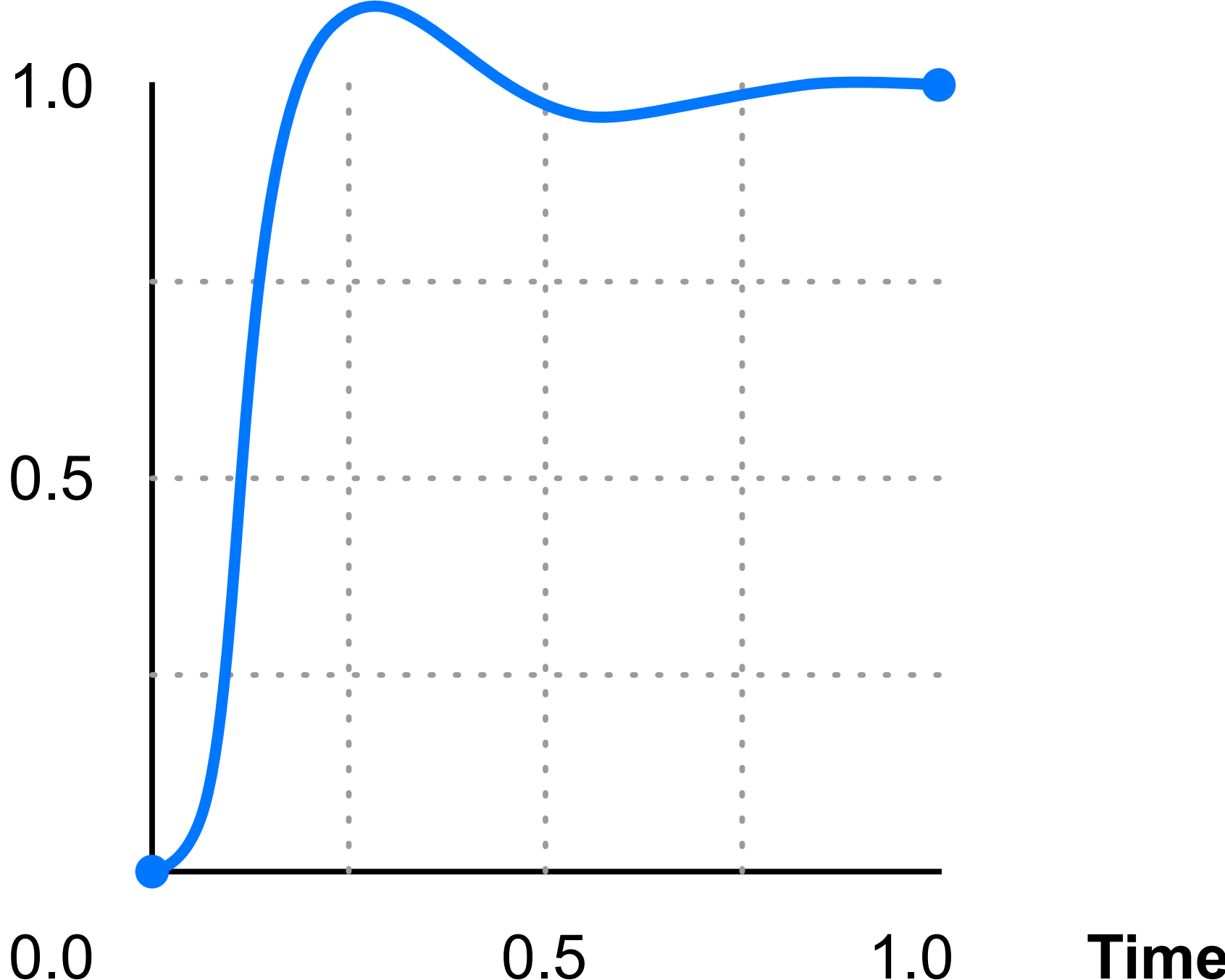
Critically Damped Spring

Damping ratio = 1.0



Underdamped Spring

Damping ratio < 1.0



Spring Animations B iOS SDK

UISpringTimingParameters

```
class UISpringTimingParameters : NSObject, UITimingCurveProvider {  
    init(dampingRatio ratio: CGFloat, initialVelocity velocity: CGVector)  
  
    init(mass: CGFloat, stiffness: CGFloat, damping: CGFloat,  
         initialVelocity velocity: CGVector)  
  
}
```

Spring Animations B iOS SDK

UISpringTimingParameters

```
let timingParameters = UISpringTimingParameters(mass: 1, stiffness: 100, damping: 10,
                                                initialVelocity: .zero)

let animator = UIViewPropertyAnimator(duration: 4, timingParameters: timingParameters)

animator.addAnimations { /* animations */ }
animator.startAnimation()

print(animator.duration) // 1.4727003346780927
```

Spring Animations B iOS SDK

UISpringTimingParameters

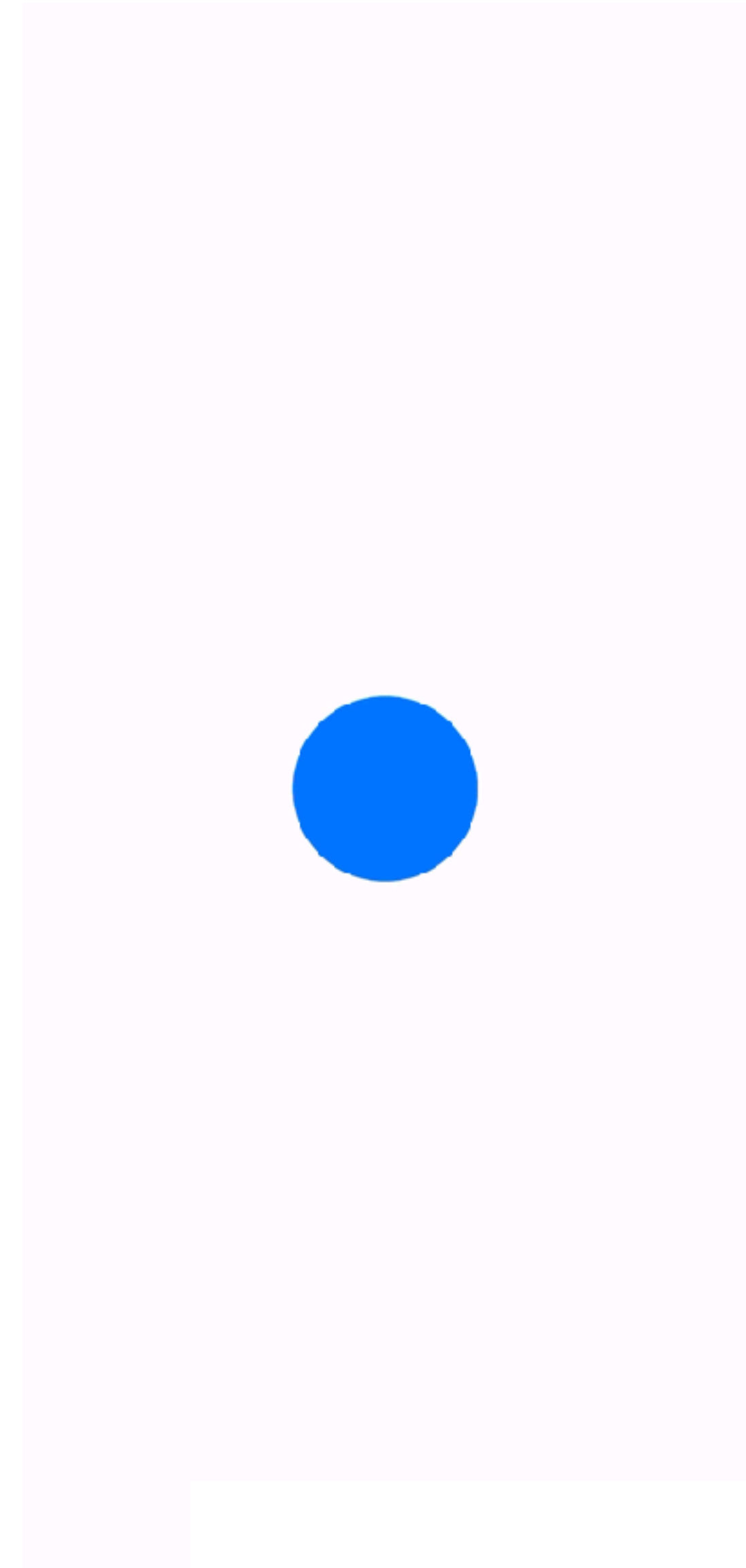
```
let timingParameters = UISpringTimingParameters(dampingRatio: 0.3,  
                                                initialVelocity: .zero)  
  
let animator = UIViewPropertyAnimator(duration: 4, timingParameters: timingParameters)  
  
print(animator.duration) // 4.0
```

Spring Animations в iOS SDK

Нулевое смещение

- › Не работает с нулевым смещением:
`fromValue == toValue`

```
UIView.animate(  
    withDuration: 5,  
    delay: 0,  
    usingSpringWithDamping: 0.1,  
    initialSpringVelocity: -1000,  
    animations: {  
        self.circle.frame = self.circle.frame  
    })
```



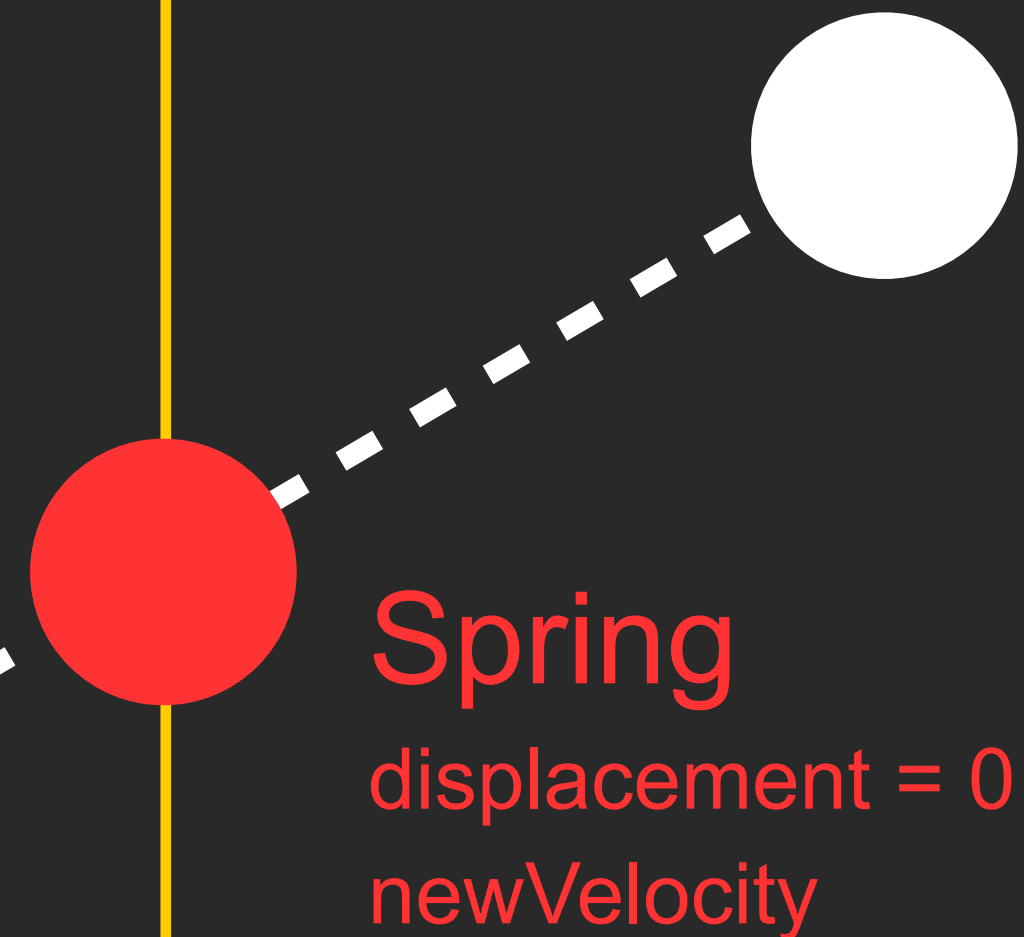
SpringTimingParameters

```
struct Spring {  
    var mass: CGFloat  
    var stiffness: CGFloat  
    var dampingRatio: CGFloat  
}  
  
struct SpringTimingParameters {  
    var spring: Spring  
    var displacement: CGPoint  
    var initialVelocity: CGPoint  
    var threshold: CGFloat  
}  
  
extension SpringTimingParameters {  
    var duration: TimeInterval  
    func value(at time: TimeInterval) -> CGPoint  
}
```

Bounce

Scheme bounds

Destination



Spring
displacement = 0
newVelocity

Finger
contentOffset
velocity

DecelerationTimingParameters

```
extension DecelerationTimingParameters {  
    func duration(to value: CGPoint) -> TimeInterval?  
    func velocity(at time: TimeInterval) -> CGPoint  
}
```

SimpleScrollView

```
@objc func handlePanRecognizer(_ sender: UIPanGestureRecognizer) {  
    switch sender.state {  
    case .began:  
        state = .dragging(initialOffset: contentOffset)  
  
    case .changed:  
        let translation = sender.translation(in: self)  
        if case .dragging(let initialOffset) = state {  
            contentOffset = clampOffset(initialOffset - translation)  
        }  
  
    case .ended:  
        state = .default  
        let velocity = sender.velocity(in: self)  
        startDeceleration(withVelocity: -velocity)  
  
    // Other cases  
    }  
}
```


SimpleScrollView

```
func startDeceleration(withVelocity velocity: CGPoint) {
    let parameters = DecelerationTimingParameters(...)

    let destination = parameters.destination
    let intersection = getIntersection(rect: contentOffsetBounds, segment: (contentOffset, destination))

    let duration: TimeInterval
    if let intersection = intersection {
        duration = parameters.duration(to: intersection)
    } else {
        duration = parameters.duration
    }

    contentOffsetAnimation = TimerAnimation(
        duration: duration,
        animations: { [weak self] _, time in
            self?.contentOffset = parameters.value(at: time)
        },
        completion: { [weak self] finished in
            guard finished && intersection != nil else { return }
            let velocity = parameters.velocity(at: duration)
            self?.bounce(withVelocity: velocity)
        })
}
```

SimpleScrollView

```
func bounce(withVelocity velocity: CGPoint) {
    let restOffset = contentOffset.clamped(to: contentOffsetBounds)
    let displacement = contentOffset - restOffset
    let threshold = 0.5 / UIScreen.main.scale
    let spring = Spring(mass: 1, stiffness: 100, dampingRatio: 1)

    let parameters = SpringTimingParameters(spring: spring,
                                            displacement: displacement,
                                            initialVelocity: velocity,
                                            threshold: threshold)

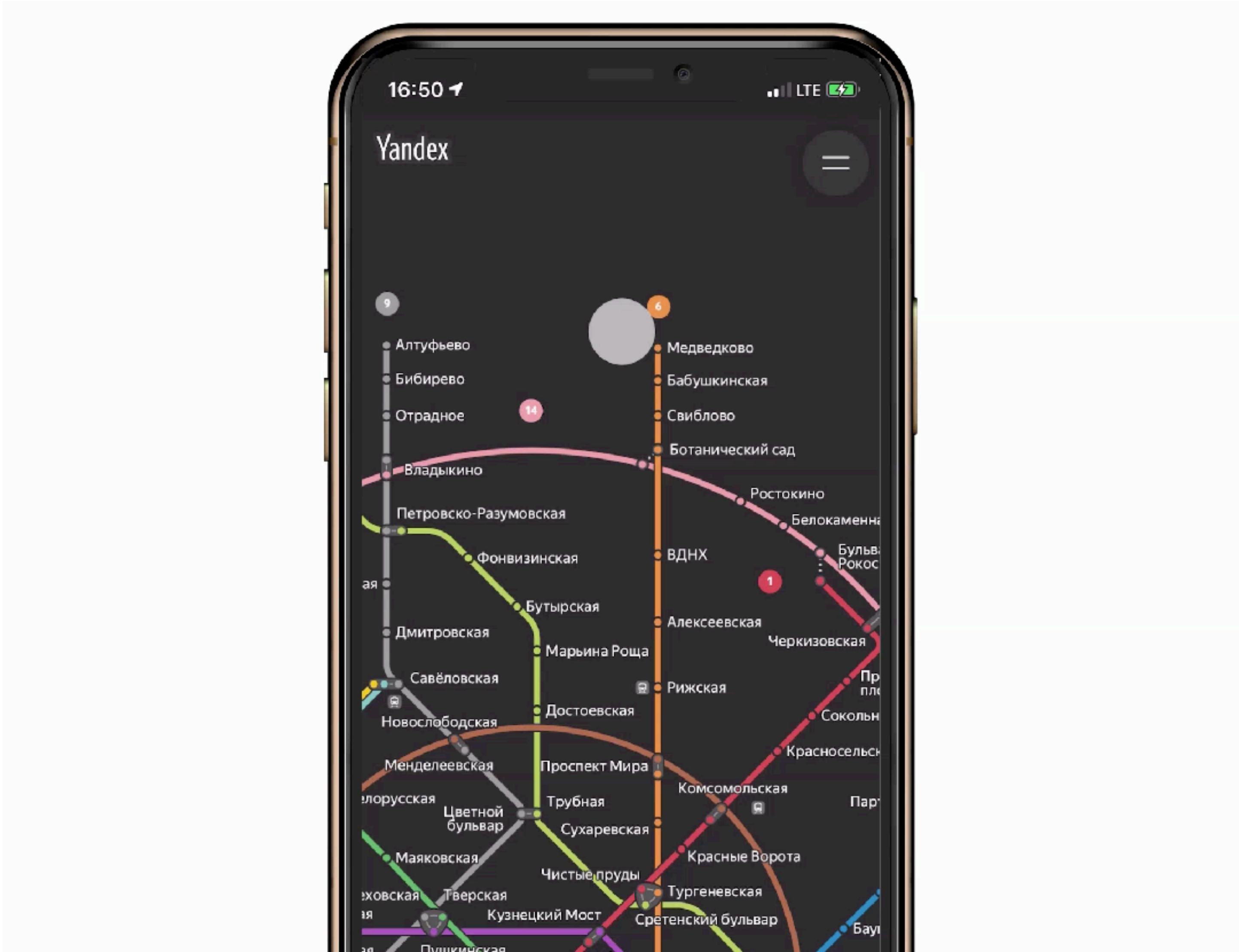
    contentOffsetAnimation = TimerAnimation(
        duration: parameters.duration,
        animations: { [weak self] _, time in
            self?.contentOffset = restOffset + parameters.value(at: time)
        })
}
```

Spring Animation

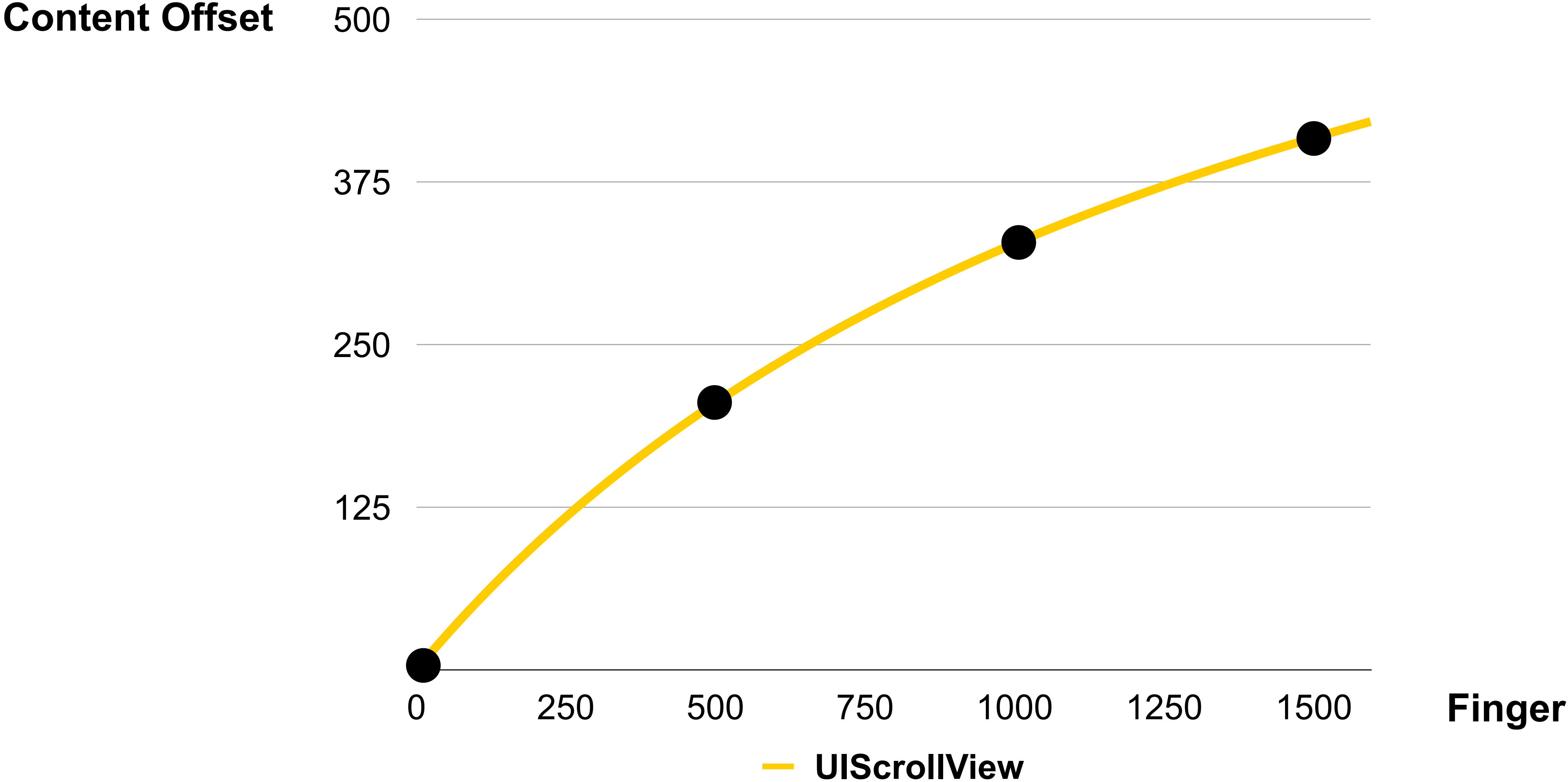


Rubber Band Effect

Rubber Band Effect



Rubber Band Effect



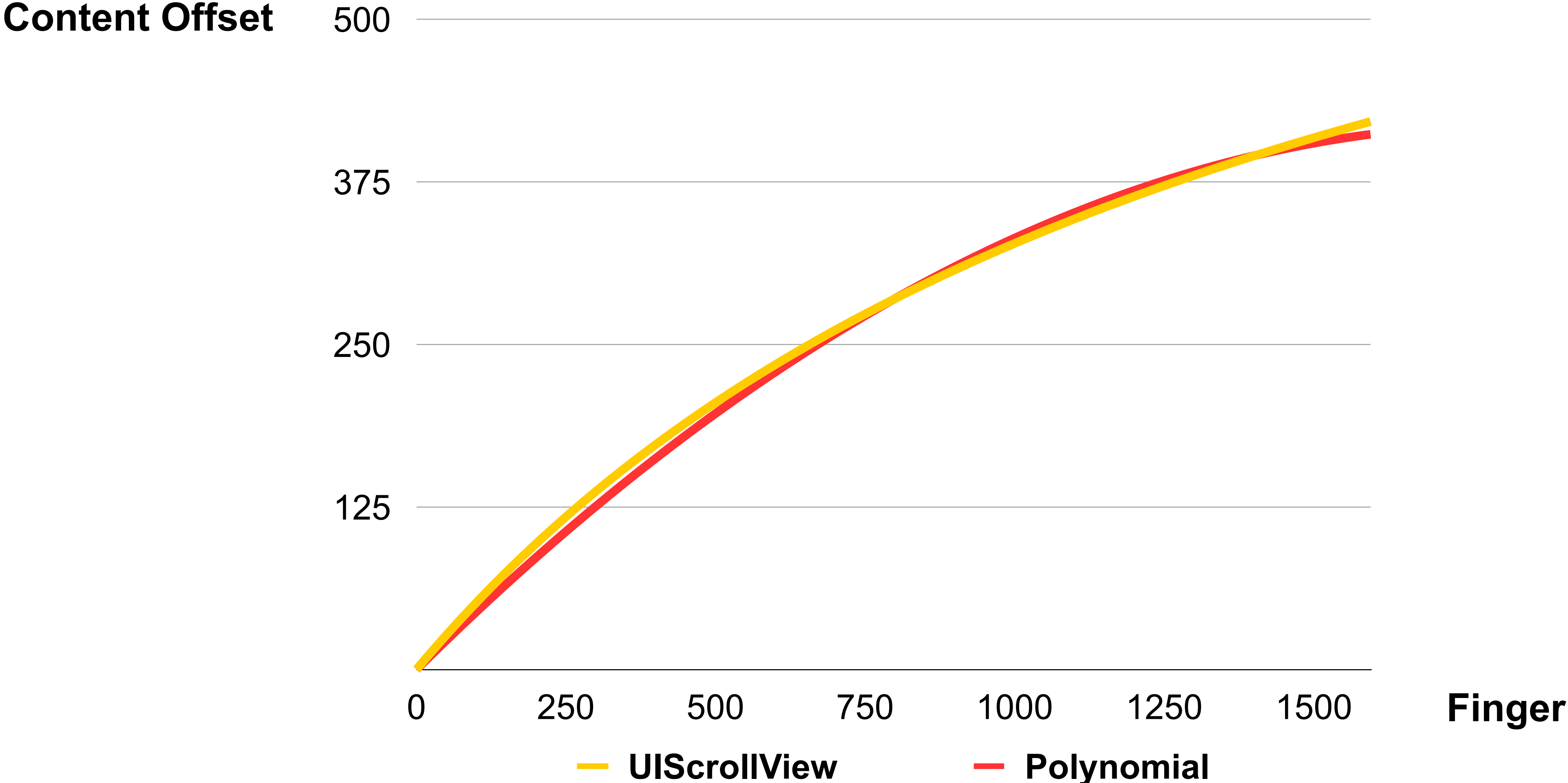
Rubber Band Effect

Полином

- › wolframalpha.com
- › quadratic fit {0, 0} {500, 205} {1000, 328} {1500, 409}

$$y = 2 + 0.456x - 0.000124x^2$$

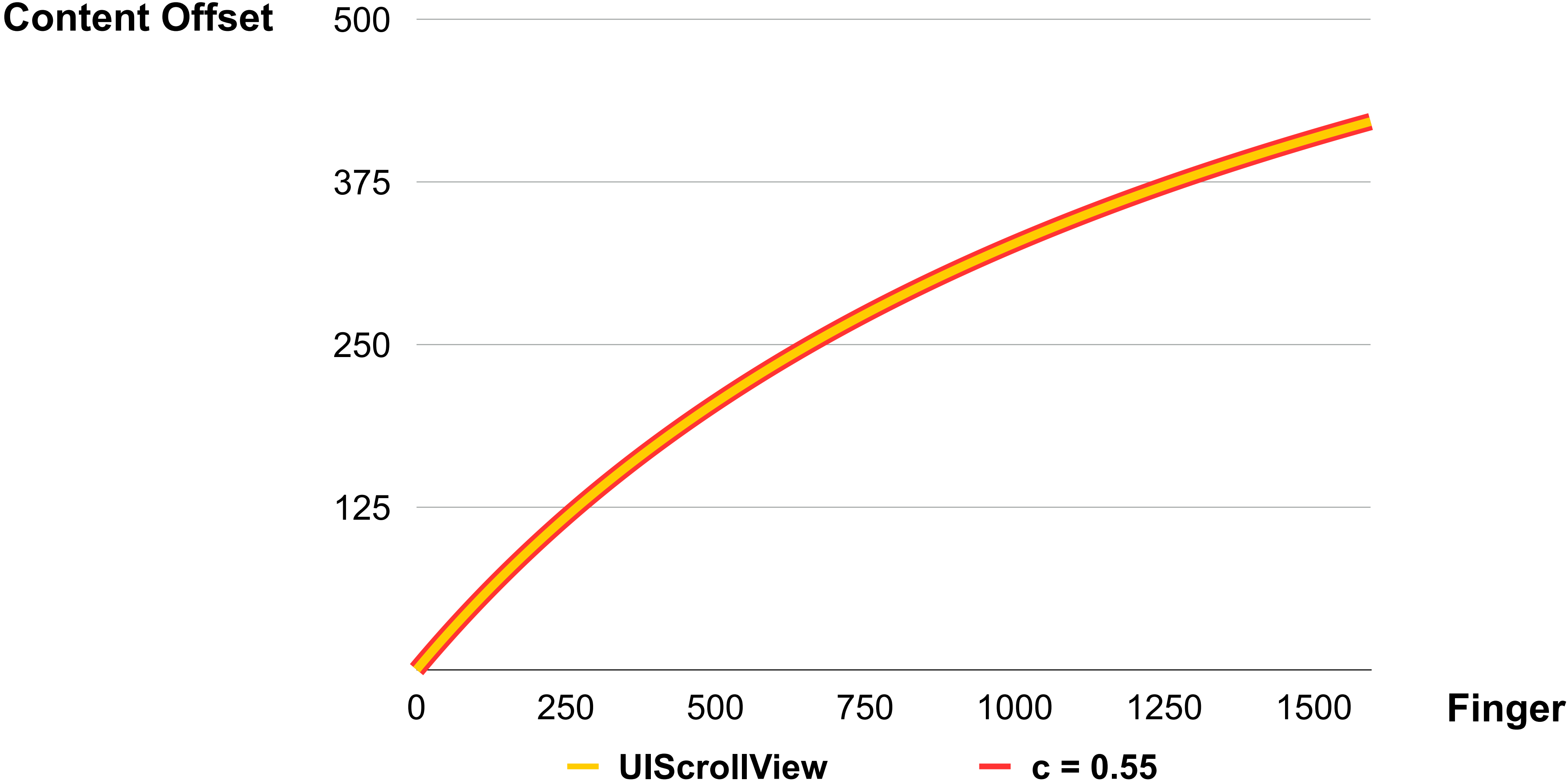
Rubber Band Effect



Rubber Band Effect



Rubber Band Effect

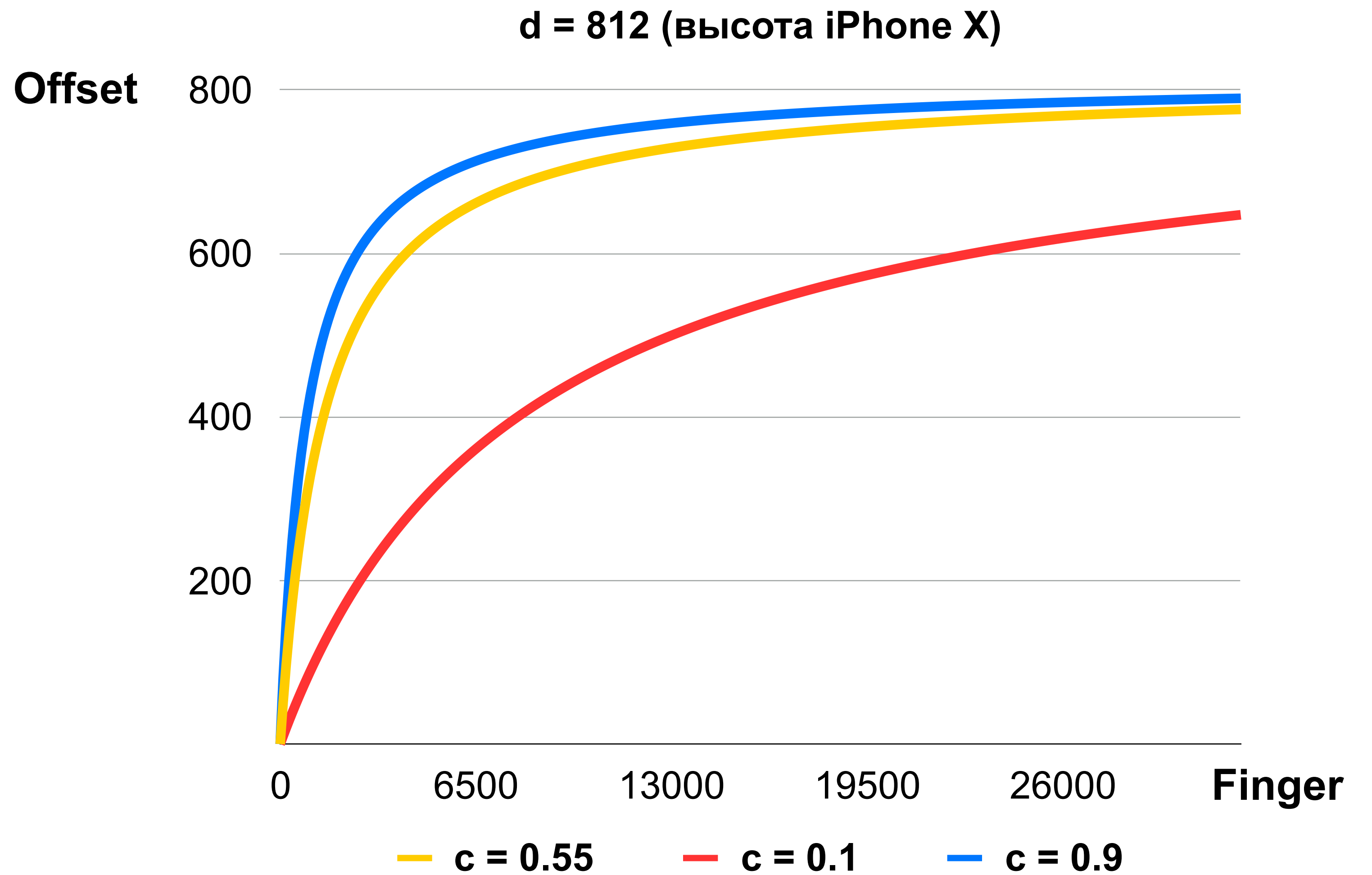


Rubber Band Effect

$$y = \left(1 - \frac{1}{\frac{cx}{d} + 1}\right)d$$

$$y \rightarrow d$$

$$y < d$$



Rubber Band Effect

```
func rubberBandClamp(_ x: CGFloat, coeff: CGFloat, dim: CGFloat) -> CGFloat {  
    return (1.0 - (1.0 / ((x * coeff / dim) + 1.0))) * dim  
}
```

Rubber Band Effect



```
func rubberBandClamp(_ x: CGFloat, coeff: CGFloat, dim: CGFloat,
                    limits: ClosedRange<CGFloat>) -> CGFloat
{
    let clampedX = x.clamped(to: limits)
    let diff = abs(x - clampedX)
    let sign: CGFloat = clampedX > x ? -1 : 1

    return clampedX + sign * rubberBandClamp(diff, coeff: coeff, dim: dim)
}
```

Rubber Band Effect

```
struct RubberBand {  
    var coeff: CGFloat = 0.55  
    var dims: CGSize  
    var bounds: CGRect  
  
    func clamp(_ point: CGPoint) -> CGPoint  
}
```

bounds

dims



SimpleScrollView

```
@objc func handlePanRecognizer(_ sender: UIPanGestureRecognizer) {  
    switch sender.state {  
    case .began:  
        state = .dragging(initialOffset: contentOffset)  
  
    case .changed:  
        let translation = sender.translation(in: self)  
        if case .dragging(let initialOffset) = state {  
            contentOffset = clampOffset(initialOffset - translation)  
        }  
  
    case .ended:  
        state = .default  
        let velocity = sender.velocity(in: self)  
        startDeceleration(withVelocity: -velocity)  
  
    // Other cases  
    }  
}
```

SimpleScrollView

```
func clampOffset(_ offset: CGPoint) -> CGPoint {  
    return offset.clamped(to: contentOffsetBounds)  
}
```


SimpleScrollView

```
func clampOffset(_ offset: CGPoint) -> CGPoint {  
    let rubberBand = RubberBand(dims: frame.size, bounds: contentOffsetBounds)  
    return rubberBand.clamp(offset)  
}
```

SimpleScrollView

```
@objc func handlePanRecognizer(_ sender: UIPanGestureRecognizer) {
    switch sender.state {
    case .began:
        state = .dragging(initialOffset: contentOffset)

    case .changed:
        let translation = sender.translation(in: self)
        if case .dragging(let initialOffset) = state {
            contentOffset = clampOffset(initialOffset - translation)
        }

    case .ended:
        state = .default
        let velocity = sender.velocity(in: self)
        startDeceleration(withVelocity: -velocity)

    // Other cases
    }
}
```

SimpleScrollView

```
@objc func handlePanRecognizer(_ sender: UIPanGestureRecognizer) {  
    switch sender.state {  
    case .began:  
        state = .dragging(initialOffset: contentOffset)  
  
    case .changed:  
        let translation = sender.translation(in: self)  
        if case .dragging(let initialOffset) = state {  
            contentOffset = clampOffset(initialOffset - translation)  
        }  
  
    case .ended:  
        state = .default  
        let velocity = sender.velocity(in: self)  
        completeGesture(withVelocity: -velocity)  
  
    // Other cases  
    }  
}
```

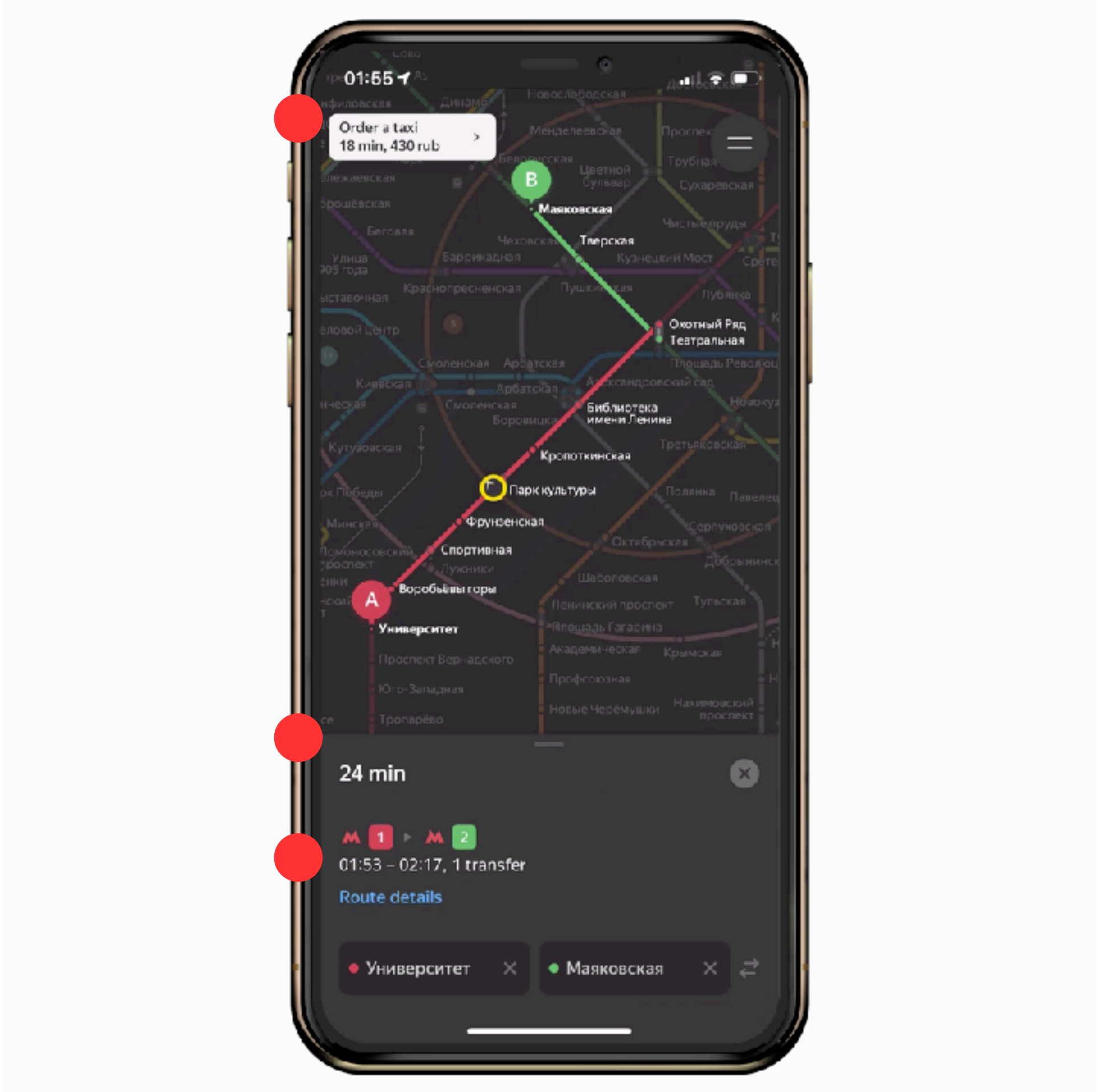
SimpleScrollView

```
func completeGesture(withVelocity velocity: CGPoint) {  
    if contentOffsetBounds.contains(contentOffset) {  
        startDeceleration(withVelocity: velocity)  
    } else {  
        bounce(withVelocity: velocity)  
    }  
}
```


Примеры

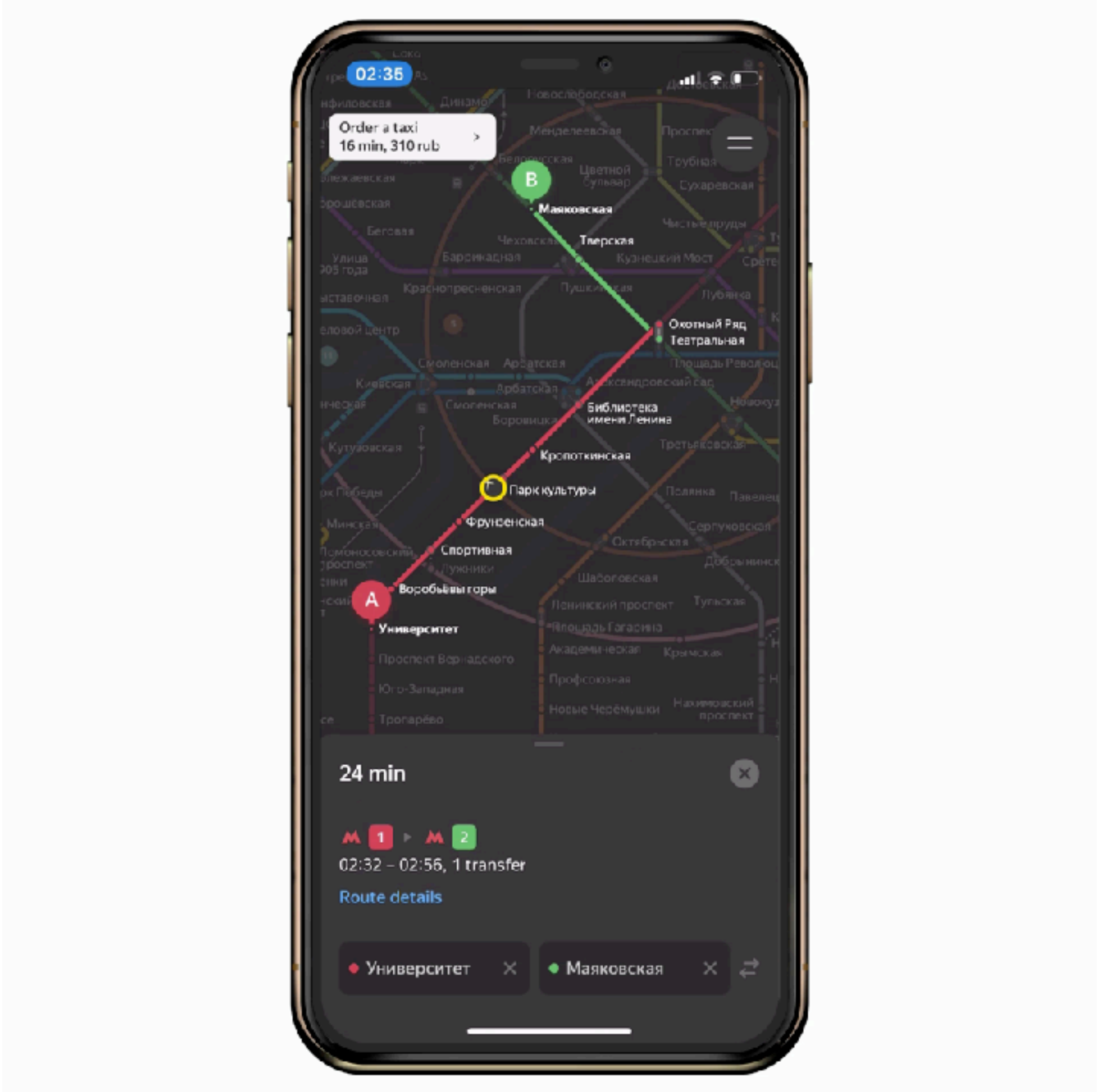
Карточка

Переход между состояниями



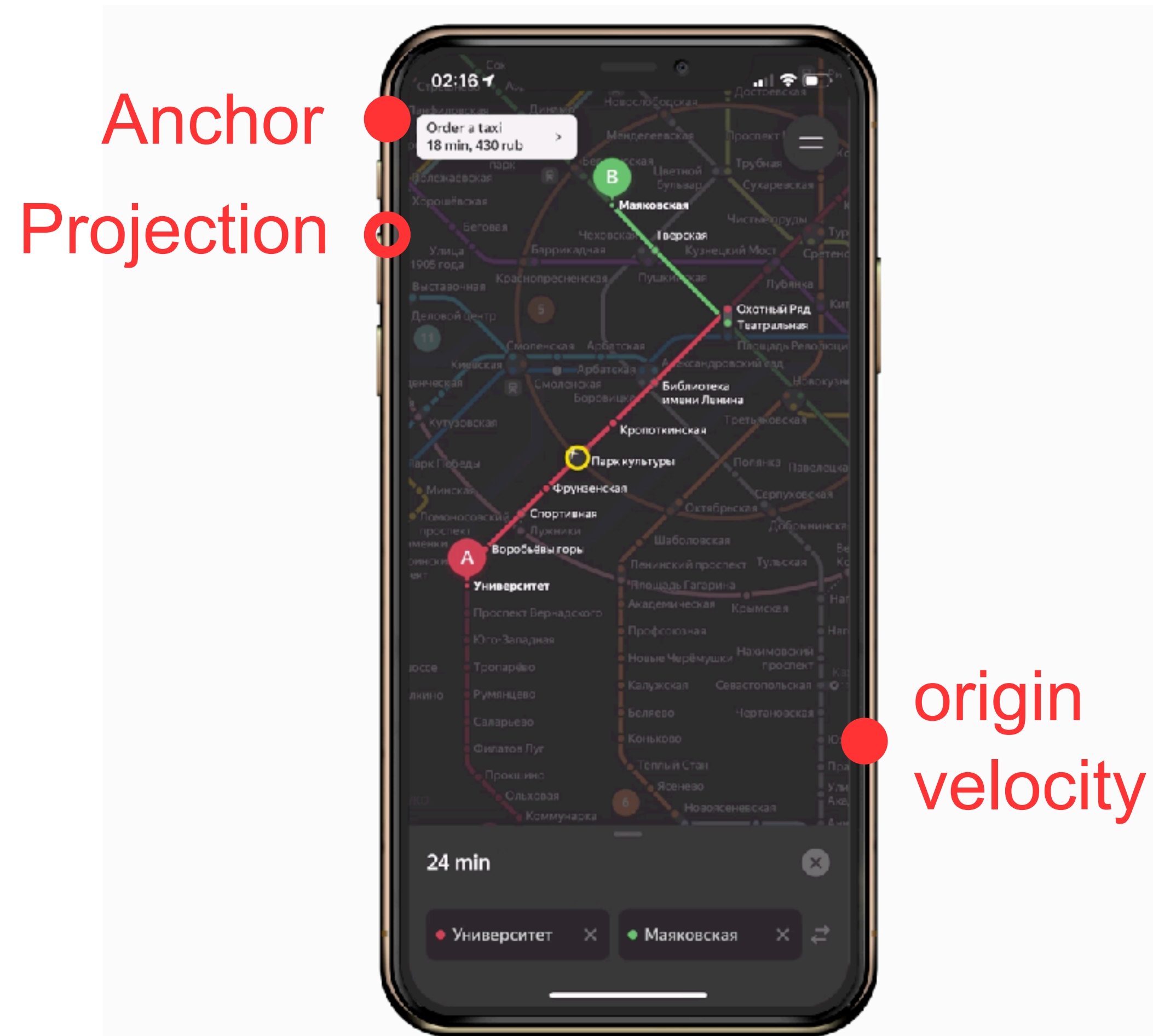
Карточка

Переход между состояниями



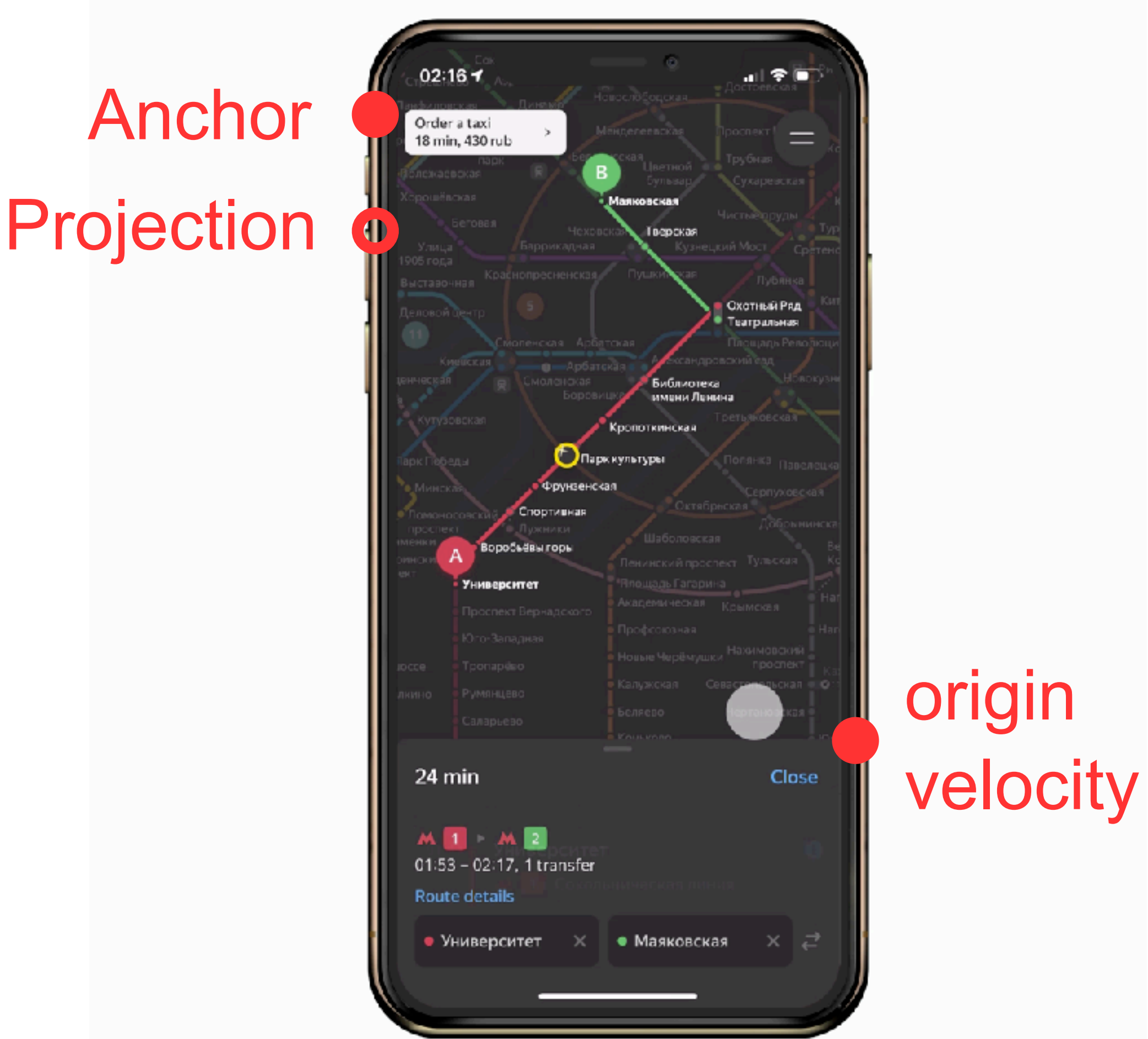
Карточка

Переход между состояниями



Карточка

Переход между состояниями



Карточка

Поиск проекции

$$X = x_0 - \frac{v_0}{1000 \ln(d)}$$

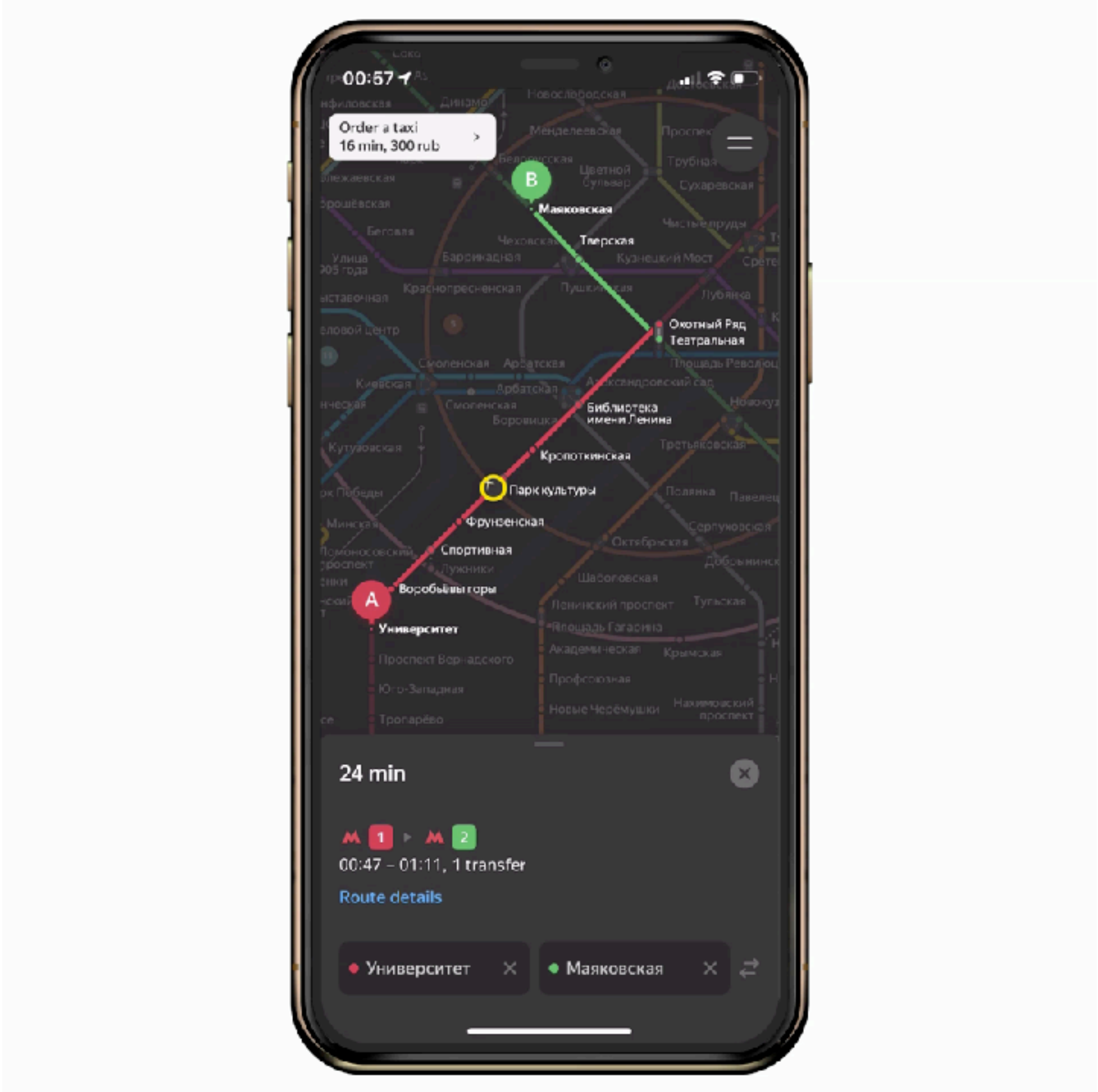
```
func project(value: CGPoint, velocity: CGPoint, decelerationRate: CGFloat) -> CGPoint {  
    return value - velocity / (1000.0 * log(decelerationRate))  
}
```

Карточка

```
func completeGesture(velocity: CGPoint) {  
    let decelerationRate = UIScrollView.DecelerationRate.normal.rawValue  
  
    let projection = project(value: self.origin, velocity: velocity,  
                             decelerationRate: decelerationRate)  
  
    let anchor = nearestAnchor(to: projection)  
  
    UIView.animate(withDuration: 0.25) { [weak self] in  
        self?.origin = anchor  
    }  
}
```

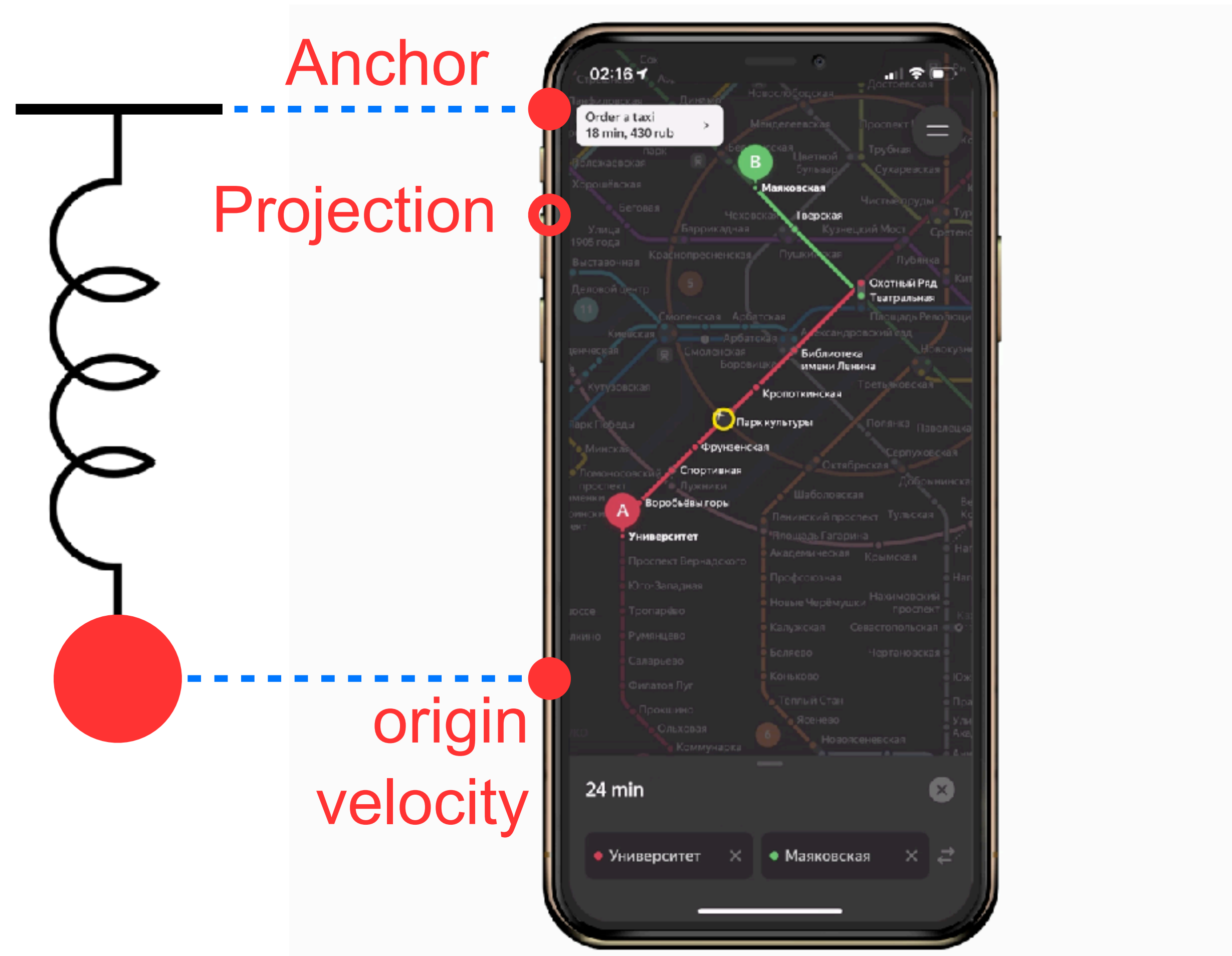
Карточка

Переход между состояниями



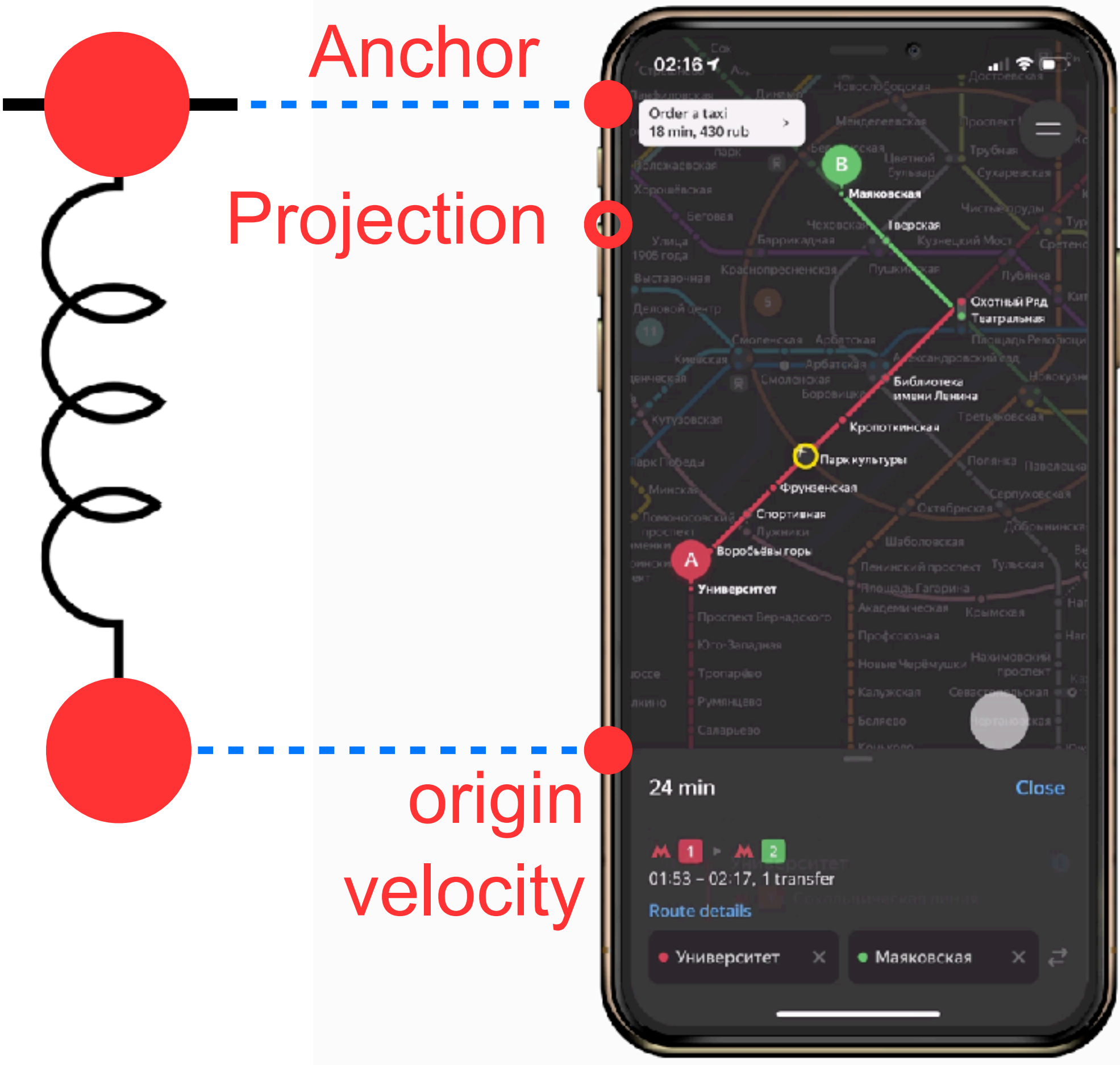
Карточка

Переход между состояниями



Карточка

Переход между состояниями



Карточка

```
func completeGesture(velocity: CGPoint) {
    let decelerationRate = UIScrollView.DecelerationRate.normal.rawValue
    let projection = project(value: self.origin, velocity: velocity,
                             decelerationRate: decelerationRate)

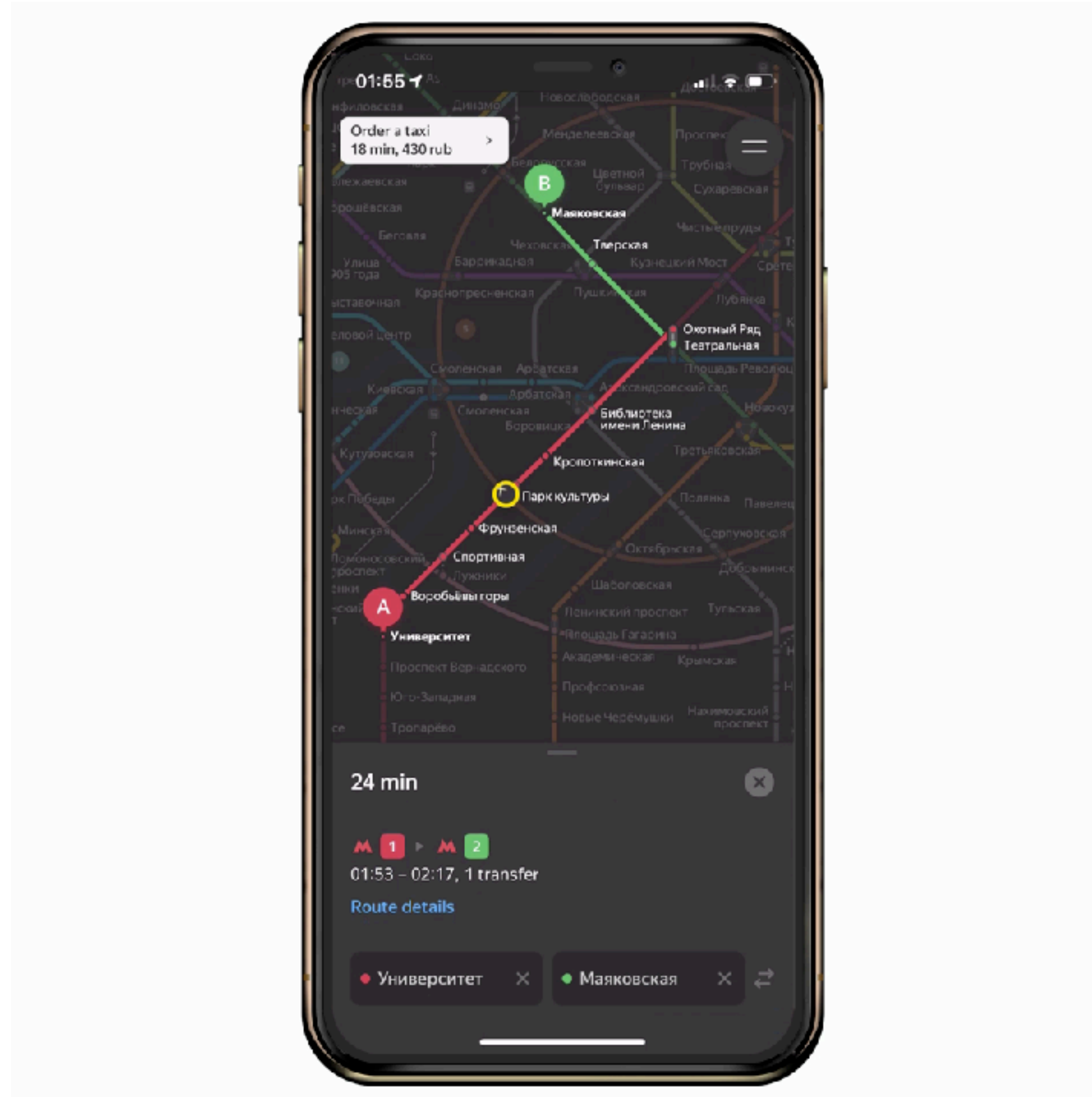
    let anchor = nearestAnchor(to: projection)

    let timingParameters = SpringTimingParameters(
        spring: Spring(mass: 1, stiffness: 200, dampingRatio: 1),
        displacement: self.origin - anchor,
        initialVelocity: velocity,
        threshold: 0.5 / UIScreen.main.scale)

    originAnimation = TimerAnimation(
        duration: timingParameters.duration,
        animations: { [weak self] _, time in
            self?.origin = anchor + timingParameters.value(at: time)
        })
}
```

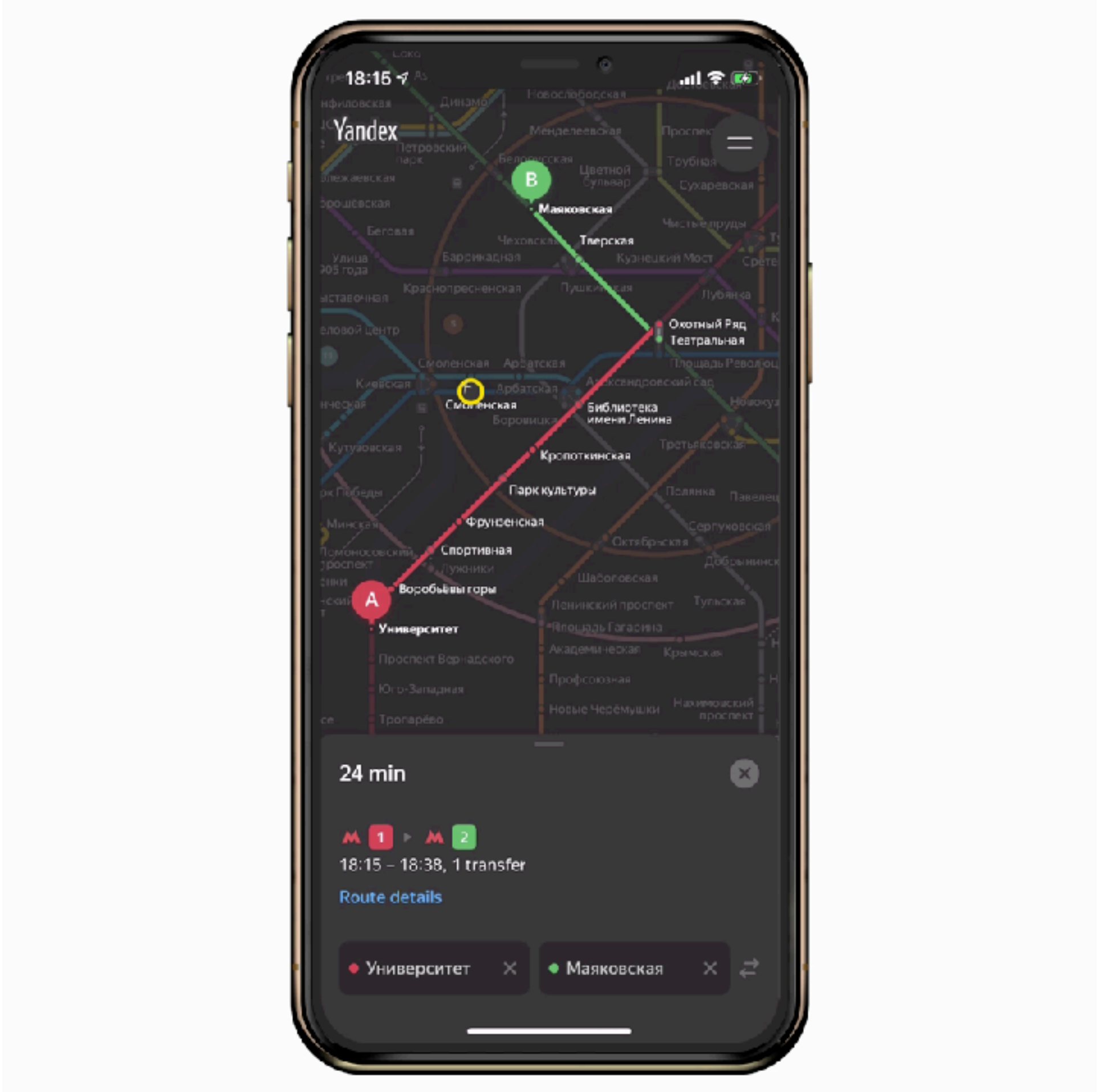

Карточка

Damping Ratio = 1.0



Карточка

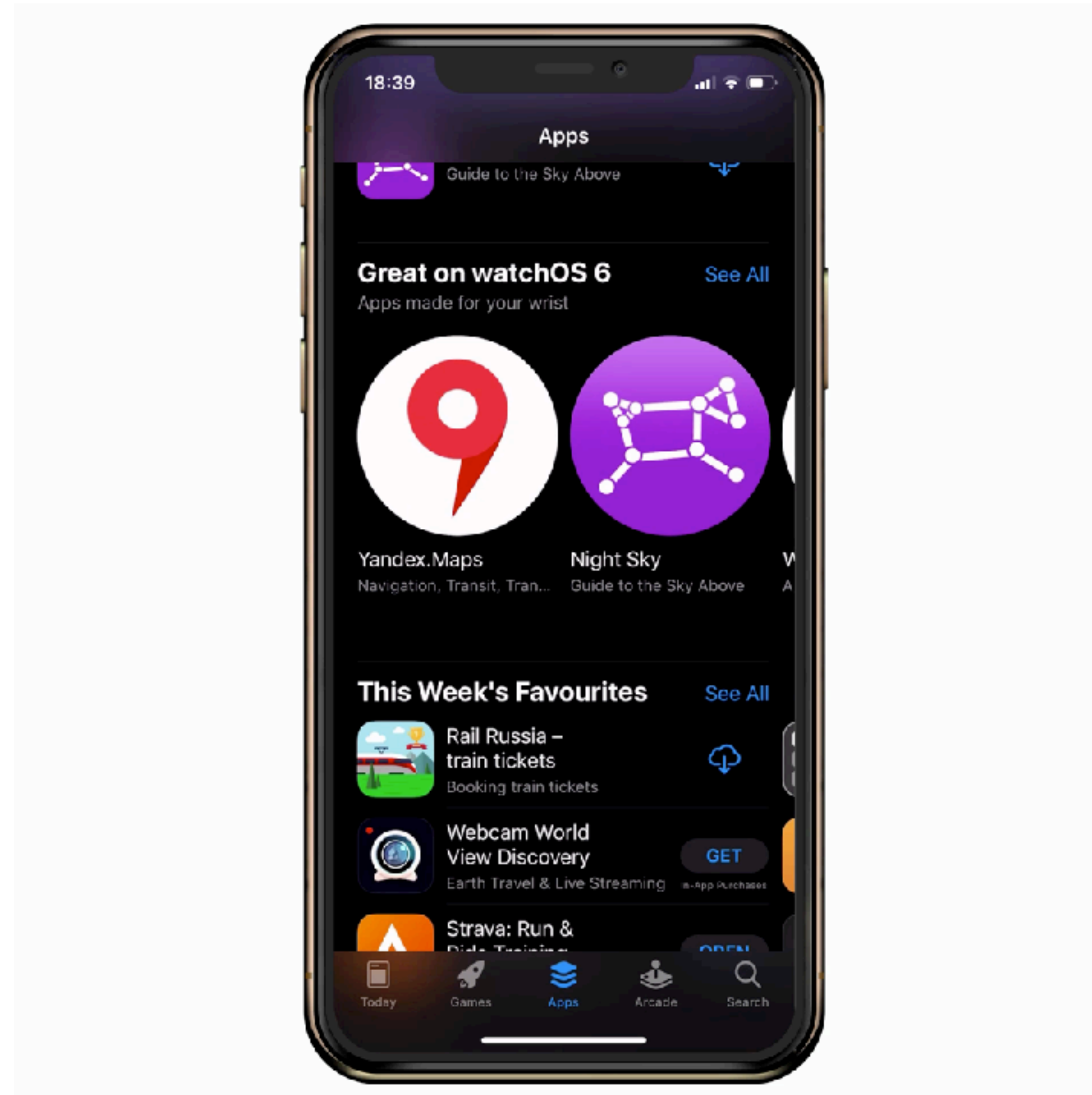
Damping Ratio < 1.0



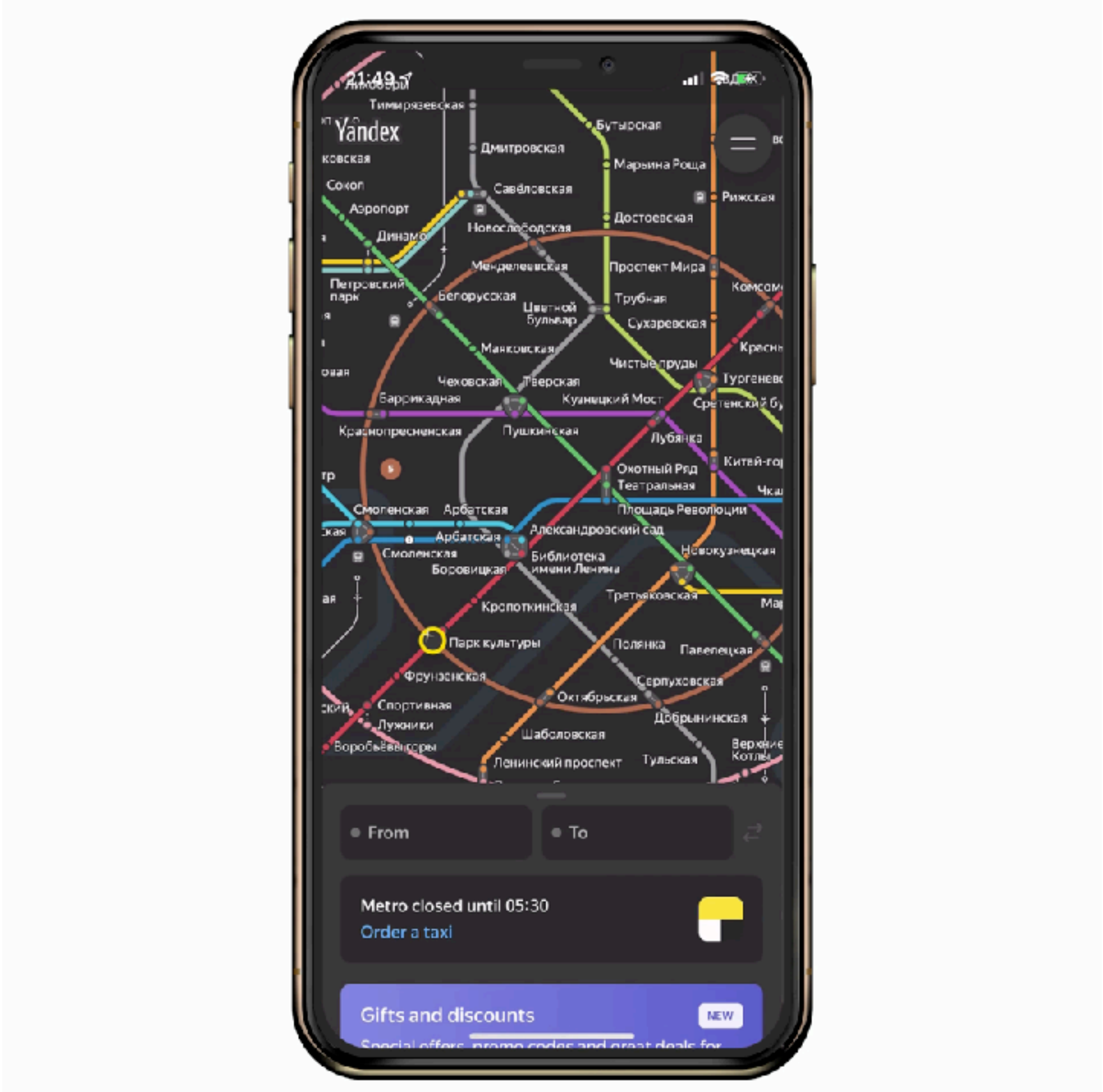
Picture in Picture



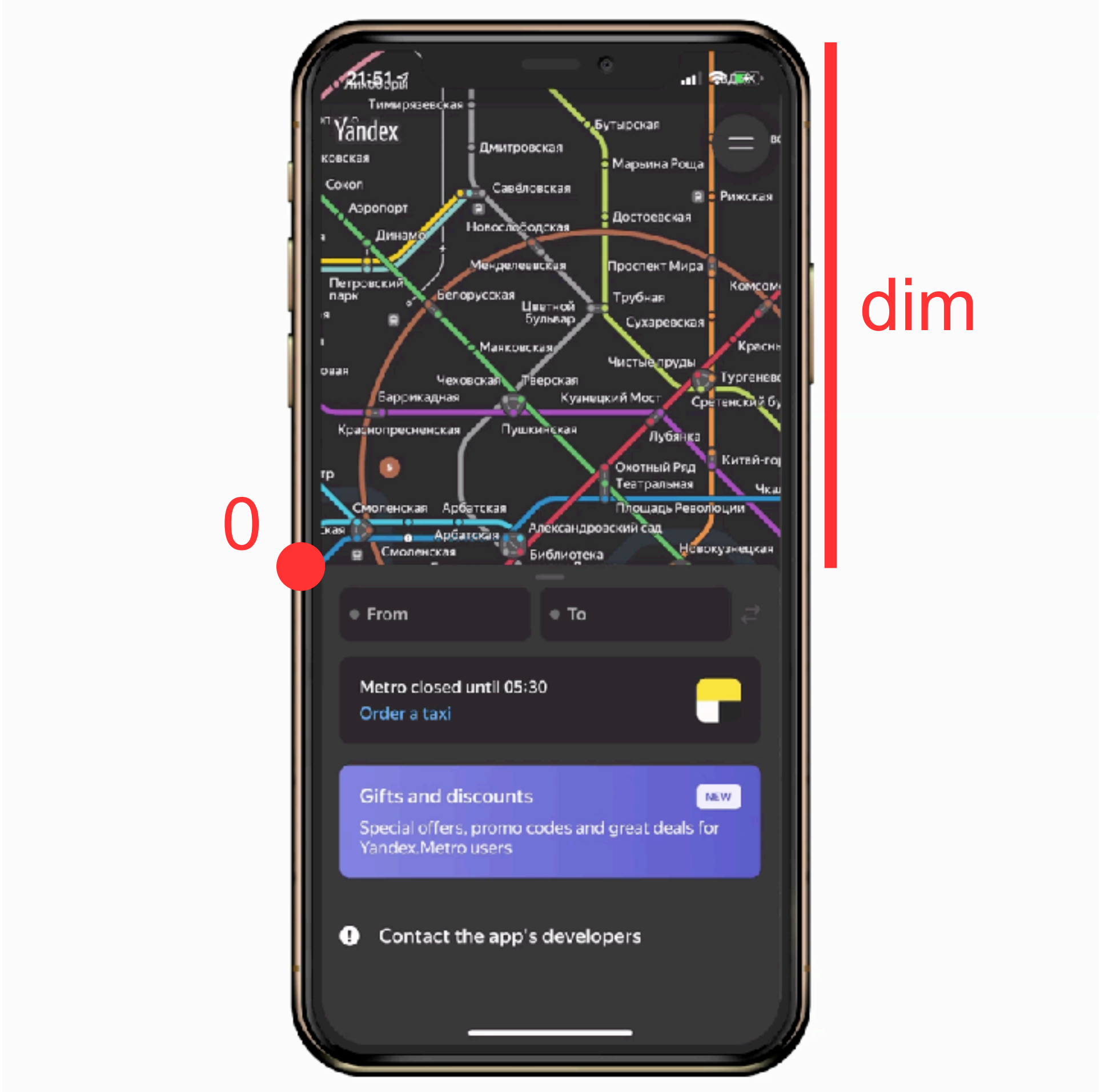
Кастомная пейджиация App Store



Карточка Rubber Band Effect



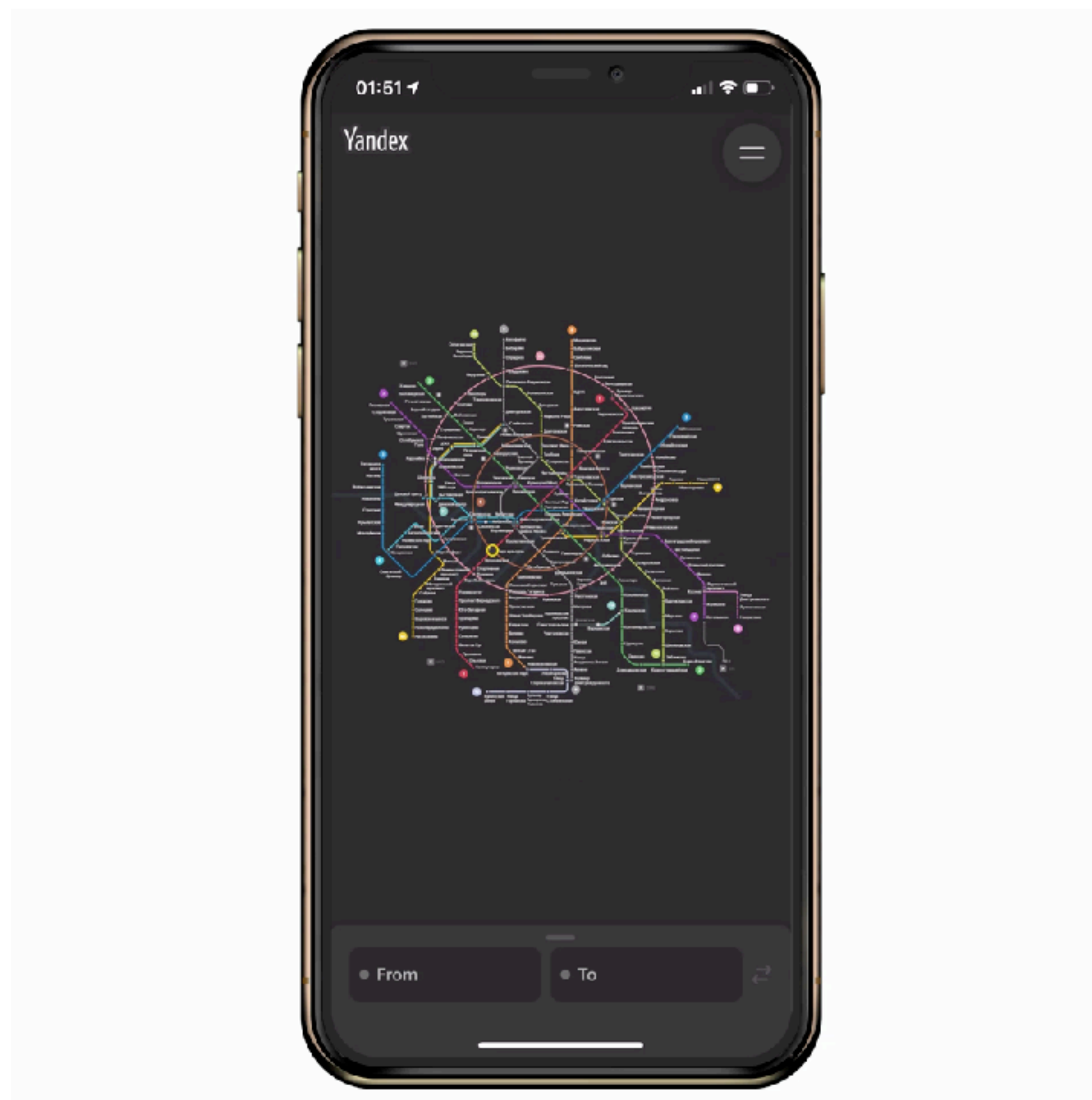
Карточка Rubber Band Effect



Карточка Rubber Band Effect



Схема Метро Scale



Заключение

Заключение

- › Плавный переход между состояниями → Проекция + Spring Animation
- › Плавная граница → Rubber Band Effect

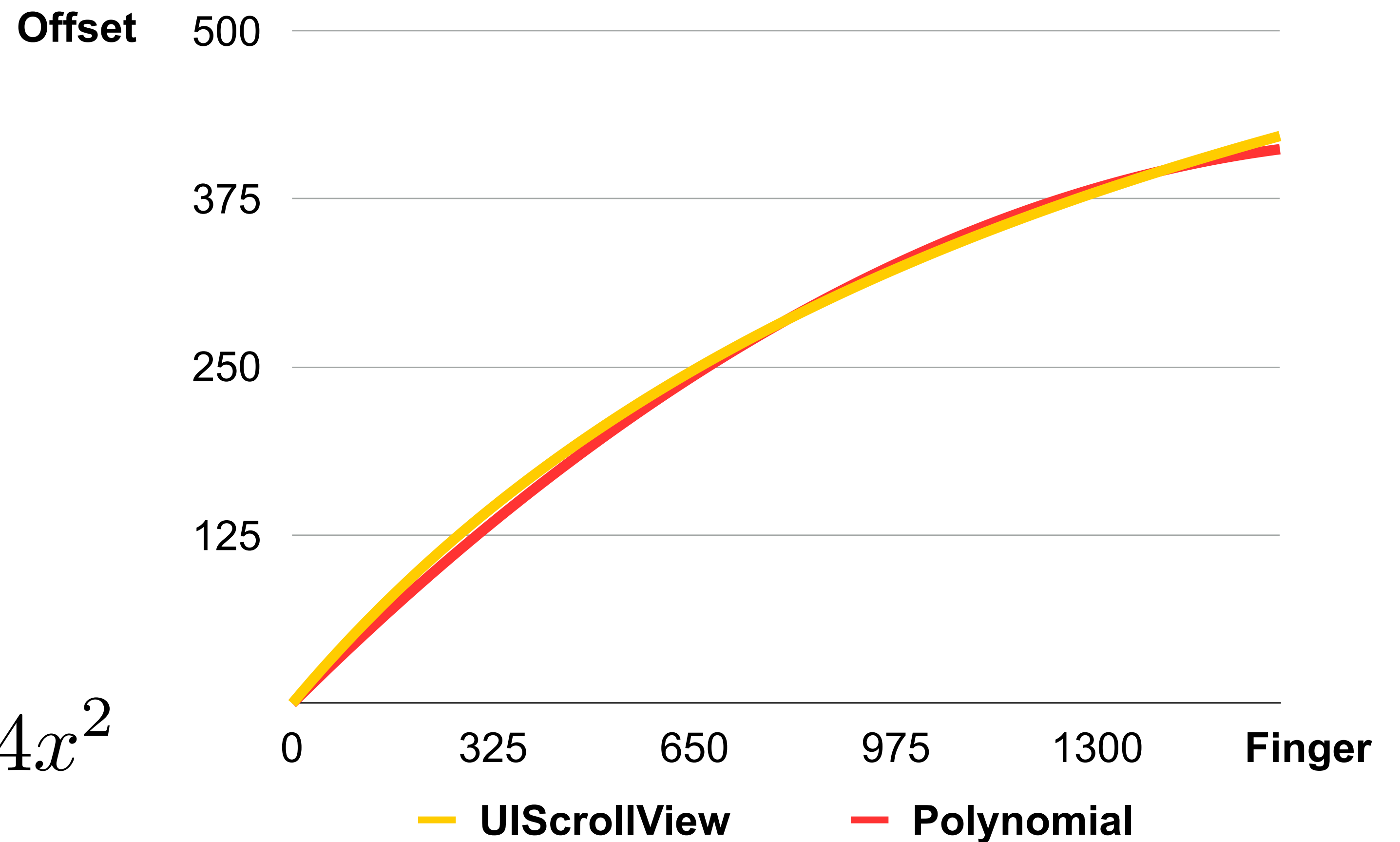
Зачем

› Rubber Band Effect

$$y = \left(1 - \frac{1}{\frac{cx}{d} + 1}\right)d$$

› Приближение

$$y = 2 + 0.456x - 0.000124x^2$$



Ссылки

- › Репозиторий с примерами
github.com/super-ultra/ScrollMechanics
- › Designing Fluid Interfaces
developer.apple.com/videos/play/wwdc2018/803
- › Advanced Animations with UIKit
developer.apple.com/videos/play/wwdc2017/230
- › Блог разработки Яндекс.Карт
medium.com/yandex-maps-ios



Спасибо

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github.com/super-ultra/ScrollMechanics



medium.com/yandex-maps-ios



medium.com/esskeetit